CE205 Data Structures

Week-3

Stacks, Queue Structures, and Related Algorithms and Problems.

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Outline-1

- Stack ADT
 - Stack Using Array
 - Stack Using Linked List
- Expressions
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 - Prefix
 - Infix to Postfix Conversion
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Outline-2

- Queue ADT
 - First Come First Serve, FCFS, FIFO
 - Queue Data structure Using Array
 - Queue Using Linked List
 - Circular Queue Data structure
 - Double Ended Queue Data structure
 - Multilevel Queue (MLQ)
- Hanoi Tower



Stack ADT

- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/stack-adt.html



Stack Data Structure

In this tutorial, you will learn about the stack data structure and its implementation in Python, Java and C/C++.

A stack is a linear data structure that follows the principle of **Last In First Out (LIFO)**. This means the last element inserted inside the stack is removed first.

You can think of the stack data structure as the pile of plates on top of another.





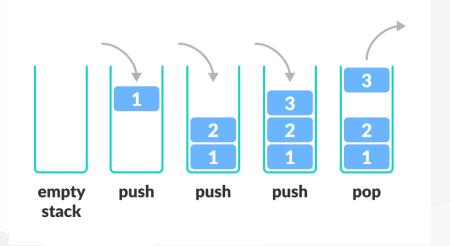
Stack Data Structure

- Stack representation similar to a pile of plate
- Here, you can:
 - Put a new plate on top
 - Remove the top plate
- And, if you want the plate at the bottom,
- You must first remove all the plates on top.
- This is exactly how the stack data structure works.



LIFO Principle of Stack

• In programming terms, putting an item on top of the stack is called **push** and removing an item is called **pop**.



- In the above image, although item 3 was kept last, it was removed first. This is exactly how the LIFO (Last In First Out) Principle works.
- We can implement a stack in any programming language like C, C++, Java, Python or C#, but the specification is pretty much the same.

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Basic Operations of Stack

- Some basic operations allow us to perform different actions on a stack.
 - Push: Add an element to the top of a stack
 - Pop: Remove an element from the top of a stack
 - IsEmpty: Check if the stack is empty
 - IsFull: Check if the stack is full
 - Peek: Get the value of the top element without removing it



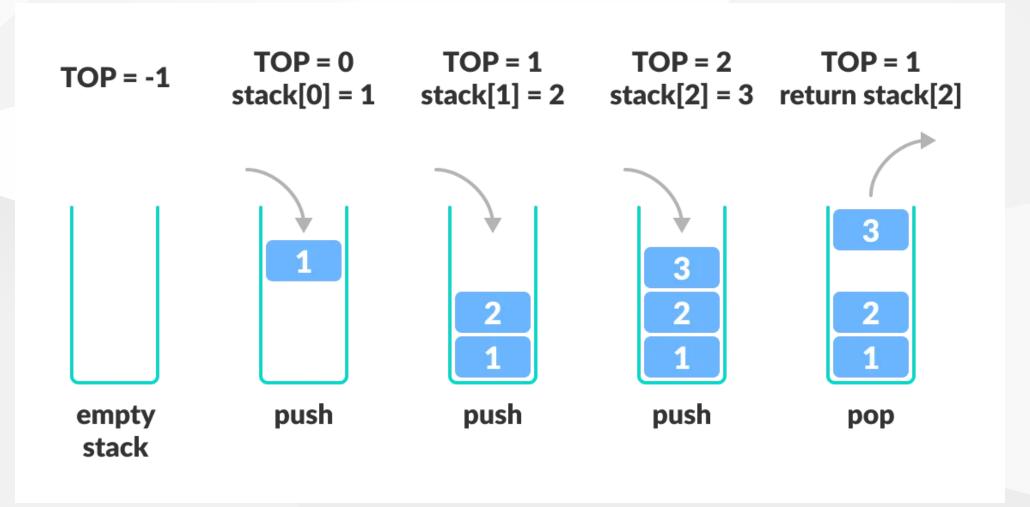
Working of Stack Data Structure

The operations work as follows:

- 1. A pointer called TOP is used to keep track of the top element in the stack.
- 2. When initializing the stack, we set its value to -1 so that we can check if the stack is empty by comparing TOP == -1.
- 3. On pushing an element, we increase the value of TOP and place the new element in the position pointed to by TOP.
- 4. On popping an element, we return the element pointed to by TOP and reduce its value.
- 5. Before pushing, we check if the stack is already full
- 6. Before popping, we check if the stack is already empty



Working of Stack Data Structure



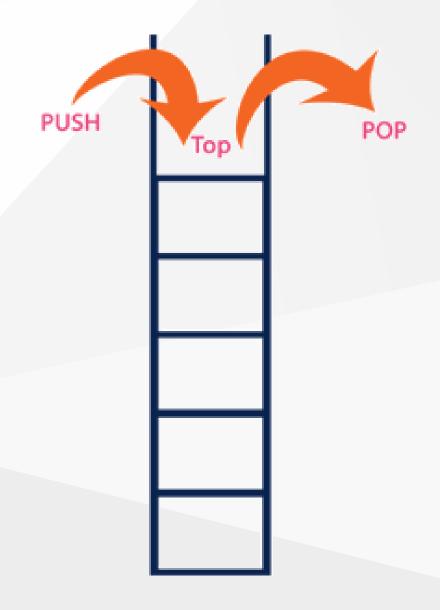
What is a Stack?

- Stack is a linear data structure in which the insertion and deletion operations are performed at only one end.
- In a stack, adding and removing of elements are performed at a single position which is known as "top".
- That means, a new element is added at top of the stack and an element is removed from the top of the stack.
- In stack, the insertion and deletion operations are performed based on **LIFO** (Last In First Out) principle.



What is a Stack?

In a stack, the insertion operation is performed using a function called "push" and deletion operation is performed using a function called "pop".





What is a Stack?

- In the figure, PUSH and POP operations are performed at a top position in the stack.
 - That means, both the insertion and deletion operations are performed at one end (i.e., at Top)
- A stack data structure can be defined as follows
- Stack is a linear data structure in which the operations are performed based on LIFO principle.
- Stack can also be defined as
 - "A Collection of similar data items in which both insertion and deletion operations are performed based on LIFO principle".



Stack Example

- If we want to create a stack by inserting 10,45,12,16,35 and 50.
- Then 10 becomes the bottom-most element and 50 is the topmost element.
- The last inserted element 50 is at Top of the stack as shown in the image below.



Stack Example





Operations on a Stack

- The following operations are performed on the stack
 - Push (To insert an element on to the stack)
 - Pop (To delete an element from the stack)
 - Display (To display elements of the stack)



Implementation of a Stack

- Stack data structure can be implemented in two ways.
 - Using Array
 - Using Linked List
- When a stack is implemented using an array, that stack can organize an only limited number of elements.
- When a stack is implemented using a linked list, that stack can organize an unlimited number of elements.



Stack Using Array

- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/stack-using-array.html



Stack Using Array

- A stack data structure can be implemented using a one-dimensional array.
- But stack implemented using array stores only a fixed number of data values. This implementation is very simple.
- Just define a one dimensional array of specific size and insert or delete the values into that array by using **LIFO principle** with the help of a variable called **'top'**.
- Initially, the top is set to -1.
- Whenever we want to insert a value into the stack, increment the top value by one and then insert.
- Whenever we want to delete a value from the stack, then delete the top value and decrement the top value by one.



- A stack can be implemented using array as follows
 - Before implementing actual operations, first follow the below steps to create an empty stack.



- Step 1 Include all the **header files** which are used in the program and define a constant **'SIZE'** with specific value.
- Step 2 Declare all the **functions** used in stack implementation.
- Step 3 Create a one dimensional array with fixed size (int stack[SIZE])
- Step 4 Define a integer variable 'top' and initialize with '-1'. (int top = -1)
- Step 5 In main method, display menu with list of operations and make suitable function calls to perform operation selected by the user on the stack.



push(value) - Inserting value into the stack

- In a stack, push() is a function used to insert an element into the stack.
- In a stack, the new element is always inserted at top position.
- Push function takes one integer value as parameter and inserts that value into the stack. We can use the following steps to push an element on to the stack



- Step 1 Check whether **stack** is **FULL**. (**top** == **SIZE-1**)
- Step 2 If it is **FULL**, then display "**Stack is FULL!!! Insertion is not possible!!!**" and terminate the function.
- Step 3 If it is **NOT FULL**, then increment **top** value by one (**top++**) and set stack[top] to value (**stack[top] = value**).



pop() - Delete a value from the Stack

- In a stack, pop() is a function used to delete an element from the stack.
- In a stack, the element is always deleted from top position.
- Pop function does not take any value as parameter.
- We can use the following steps to pop an element from the stack



- Step 1 Check whether **stack** is **EMPTY**. (**top** == **-1**)
- Step 2 If it is **EMPTY**, then display "**Stack is EMPTY!!! Deletion is not possible!!!**" and terminate the function.
- Step 3 If it is **NOT EMPTY**, then delete **stack[top]** and decrement **top** value by one (**top**--).



display() - Displays the elements of a Stack

- We can use the following steps to display the elements of a stack
 - Step 1 Check whether stack is EMPTY. (top == -1)
 - Step 2 If it is EMPTY, then display "Stack is EMPTY!!!" and terminate the function.
 - Step 3 If it is NOT EMPTY, then define a variable 'i' and initialize with top.
 Display stack[i] value and decrement i value by one (i--).
 - Step 3 Repeat above step until i value becomes '0'.



```
#include<stdio.h>
#include<conio.h>

#define SIZE 10

void push(int);
void pop();
void display();
...
```



```
int stack[SIZE], top = -1;
...
```



```
. . .
void main()
   int value, choice;
   clrscr();
   while(1){
      printf("\n\n***** MENU *****\n");
      printf("1. Push\n2. Pop\n3. Display\n4. Exit");
      printf("\nEnter your choice: ");
      scanf("%d",&choice);
      switch(choice){
     case 1: printf("Enter the value to be insert: ");
         scanf("%d",&value);
         push(value);
         break;
     case 2: pop();
         break;
     case 3: display();
         break;
     case 4: exit(0);
     default: printf("\nWrong selection!!! Try again!!!");
```

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```
void push(int value){
   if(top == SIZE-1)
      printf("\nStack is Full!!! Insertion is not possible!!!");
   else{
      top++;
      stack[top] = value;
      printf("\nInsertion success!!!");
```

```
void pop(){
   if(top == -1)
      printf("\nStack is Empty!!! Deletion is not possible!!!");
   else{
      printf("\nDeleted : %d", stack[top]);
      top--;
```

```
void display(){
   if(top == -1)
      printf("\nStack is Empty!!!");
   else{
      int i;
      printf("\nStack elements are:\n");
      for(i=top; i>=0; i--)
     printf("%d\n",stack[i]);
```



Output

```
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 Turbo C++ IDE
3. Display
4. Exit
Enter your choice: 1
Enter the value to be insert: 20
Insertion success!!!
***** MENU *****
1. Push
2. Pop
3. Display
4. Exit
Enter your choice: 3
Stack elements are:
20
10
**** MENU ****
1. Push
2. Pop
3. Display
4. Exit
Enter your choice:
```



```
// Stack implementation in Java

class Stack {
  private int arr[];
  private int top;
  private int capacity;
...
```



```
// Creating a stack
Stack(int size) {
   arr = new int[size];
   capacity = size;
   top = -1;
}
```

```
// Add elements into stack
public void push(int x) {
  if (isFull()) {
   System.out.println("OverFlow\nProgram Terminated\n");
   System.exit(1);
  System.out.println("Inserting " + x);
  arr[++top] = x;
```



```
// Remove element from stack
public int pop() {
   if (isEmpty()) {
      System.out.println("STACK EMPTY");
      System.exit(1);
   }
   return arr[top--];
}
```



```
// Utility function to return the size of the stack
public int size() {
   return top + 1;
}
```



```
// Check if the stack is empty
public Boolean isEmpty() {
   return top == -1;
}
```



```
// Check if the stack is full
public Boolean isFull() {
  return top == capacity - 1;
}
```



```
public void printStack() {
   for (int i = 0; i <= top; i++) {
      System.out.println(arr[i]);
   }
}</pre>
```

```
public static void main(String[] args) {
  Stack stack = new Stack(5);
  stack.push(1);
  stack.push(2);
  stack.push(3);
  stack.push(4);
  stack.pop();
  System.out.println("\nAfter popping out");
  stack.printStack();
```

```
// Stack implementation in C
#include <stdio.h>
#include <stdlib.h>
#define MAX 10
int count = 0;
// Creating a stack
struct stack {
  int items[MAX];
  int top;
typedef struct stack st;
. . .
```

```
// Stack implementation in C

void createEmptyStack(st *s) {
  s->top = -1;
}
...
```

```
// Check if the stack is full
int isfull(st *s) {
  if (s->top == MAX - 1)
    return 1;
  else
    return 0;
}
```



```
// Check if the stack is empty
int isempty(st *s) {
  if (s->top == -1)
    return 1;
  else
    return 0;
}
```

```
// Add elements into stack
void push(st *s, int newitem) {
  if (isfull(s)) {
    printf("STACK FULL");
  } else {
    s->top++;
    s->items[s->top] = newitem;
  count++;
. . .
```



```
// Remove element from stack
void pop(st *s) {
  if (isempty(s)) {
    printf("\n STACK EMPTY \n");
  } else {
    printf("Item popped= %d", s->items[s->top]);
    s->top--;
  count--;
  printf("\n");
```

```
// Print elements of stack
void printStack(st *s) {
  printf("Stack: ");
  for (int i = 0; i < count; i++) {</pre>
    printf("%d ", s->items[i]);
  printf("\n");
```



```
. . .
// Driver code
int main() {
  int ch;
  st *s = (st *)malloc(sizeof(st));
  createEmptyStack(s);
  push(s, 1);
  push(s, 2);
  push(s, 3);
  push(s, 4);
  printStack(s);
  pop(s);
  printf("\nAfter popping out\n");
  printStack(s);
```

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```
// Stack implementation in C++
#include <stdlib.h>
#include <iostream>
using namespace std;
#define MAX 10
int size = 0;
// Creating a stack
struct stack {
  int items[MAX];
  int top;
typedef struct stack st;
. . .
```

```
void createEmptyStack(st *s) {
  s->top = -1;
}
...
```



```
// Check if the stack is full
int isfull(st *s) {
   if (s->top == MAX - 1)
     return 1;
   else
     return 0;
}
```



```
// Check if the stack is empty
int isempty(st *s) {
  if (s->top == -1)
    return 1;
  else
    return 0;
}
```



```
// Add elements into stack
void push(st *s, int newitem) {
  if (isfull(s)) {
    cout << "STACK FULL";</pre>
  } else {
    s->top++;
    s->items[s->top] = newitem;
  size++;
```



```
// Remove element from stack
void pop(st *s) {
  if (isempty(s)) {
    cout << "\n STACK EMPTY \n";</pre>
  } else {
    cout << "Item popped= " << s->items[s->top];
    s->top--;
  size--;
  cout << endl;</pre>
```

```
// Print elements of stack
void printStack(st *s) {
   printf("Stack: ");
   for (int i = 0; i < size; i++) {
      cout << s->items[i] << " ";
   }
   cout << endl;
}</pre>
```

```
// Driver code
int main() {
  int ch;
  st *s = (st *)malloc(sizeof(st));
  createEmptyStack(s);
  push(s, 1);
  push(s, 2);
  push(s, 3);
 push(s, 4);
  printStack(s);
  pop(s);
  cout << "\nAfter popping out\n";</pre>
  printStack(s);
```

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Stack Time Complexity

For the array-based implementation of a stack, the push and pop operations take constant time, i.e. 0(1).



Applications of Stack Data Structure

- Although stack is a simple data structure to implement, it is very powerful. The most common uses of a stack are:
 - To reverse a word Put all the letters in a stack and pop them out. Because of the LIFO order of stack, you will get the letters in reverse order.
 - In compilers Compilers use the stack to calculate the value of expressions like 2 + 4 / 5 * (7 9) by converting the expression to prefix or postfix form.
 - In browsers The back button in a browser saves all the URLs you have visited previously in a stack. Each time you visit a new page, it is added on top of the stack. When you press the back button, the current URL is removed from the stack, and the previous URL is accessed.



Stack Using Linked List

- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/stack-using-linked-list.html



Stack Using Linked List

- The major problem with the stack implemented using an array is, it works only for a fixed number of data values.
- That means the amount of data must be specified at the beginning of the implementation itself.
- Stack implemented using an array is not suitable, when we don't know the size of data which we are going to use.
- A stack data structure can be implemented by using a linked list data structure. The stack implemented using linked list can work for an unlimited number of values.
- That means, stack implemented using linked list works for the variable size of data. So, there is no need to fix the size at the beginning of the implementation. The Stack implemented using linked list can organize as many data values as we want.

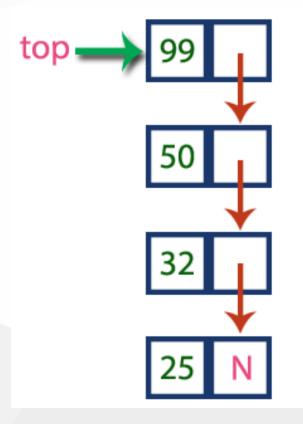


Stack Using Linked List

In linked list implementation of a stack, every new element is inserted as 'top' element. That means every newly inserted element is pointed by 'top'. Whenever we want to remove an element from the stack, simply remove the node which is pointed by 'top' by moving 'top' to its previous node in the list. The next field of the first element must be always NULL.



Stack Using Linked List Example



• In the above example, the last inserted node is 99 and the first inserted node is 25. The order of elements inserted is 25, 32,50 and 99.



- To implement a stack using a linked list, we need to set the following things before implementing actual operations.
 - Step 1 Include all the header files which are used in the program. And declare all the user defined functions.
 - Step 2 Define a 'Node' structure with two members data and next.
 - Step 3 Define a Node pointer 'top' and set it to NULL.
 - Step 4 Implement the main method by displaying Menu with list of operations and make suitable function calls in the main method.



- push(value) Inserting an element into the Stack
- We can use the following steps to insert a new node into the stack...
 - Step 1 Create a newNode with given value.
 - Step 2 Check whether stack is Empty (top == NULL)
 - Step 3 If it is Empty, then set newNode → next = NULL.
 - Step 4 If it is Not Empty, then set newNode → next = top.
 - Step 5 Finally, set top = newNode.



- pop() Deleting an Element from a Stack
- We can use the following steps to delete a node from the stack...
 - Step 1 Check whether stack is Empty (top == NULL).
 - Step 2 If it is Empty, then display "Stack is Empty!!! Deletion is not possible!!!" and terminate the function
 - Step 3 If it is Not Empty, then define a Node pointer 'temp' and set it to 'top'.
 - Step 4 Then set 'top = top \rightarrow next'.
 - Step 5 Finally, delete 'temp'. (free(temp)).



- display() Displaying stack of elements
- We can use the following steps to display the elements (nodes) of a stack...
 - Step 1 Check whether stack is Empty (top == NULL).
 - Step 2 If it is Empty, then display 'Stack is Empty!!!' and terminate the function.
 - Step 3 If it is **Not Empty**, then define a Node pointer 'temp' and initialize with top.
 - Step 4 Display 'temp → data --->' and move it to the next node. Repeat the same until temp reaches to the first node in the stack. (temp → next != NULL).
 - Step 5 Finally! Display 'temp → data ---> NULL'.



```
#include<stdio.h>
#include<conio.h>

struct Node
{
   int data;
   struct Node *next;
}*top = NULL;
...
```



```
void push(int);
void pop();
void display();
...
```



```
. . .
void main()
   int choice, value;
   clrscr();
   printf("\n:: Stack using Linked List ::\n");
   while(1){
      printf("\n***** MENU *****\n");
      printf("1. Push\n2. Pop\n3. Display\n4. Exit\n");
      printf("Enter your choice: ");
      scanf("%d",&choice);
      switch(choice){
     case 1: printf("Enter the value to be insert: ");
         scanf("%d", &value);
         push(value);
         break;
     case 2: pop(); break;
     case 3: display(); break;
     case 4: exit(0);
     default: printf("\nWrong selection!!! Please try again!!!\n");
```

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```
void push(int value)
   struct Node *newNode;
   newNode = (struct Node*)malloc(sizeof(struct Node));
   newNode->data = value;
   if(top == NULL)
      newNode->next = NULL;
   else
      newNode->next = top;
   top = newNode;
   printf("\nInsertion is Success!!!\n");
```

Stack using Linked List in C

```
void pop()
   if(top == NULL)
      printf("\nStack is Empty!!!\n");
   else{
      struct Node *temp = top;
      printf("\nDeleted element: %d", temp->data);
      top = temp->next;
      free(temp);
```

Stack using Linked List in C

```
void display()
   if(top == NULL)
      printf("\nStack is Empty!!!\n");
   else{
      struct Node *temp = top;
      while(temp->next != NULL){
     printf("%d--->",temp->data);
     temp = temp -> next;
      printf("%d--->NULL",temp->data);
```



Output

```
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C:\WINDOWS\system32\cmd.exe - tc
:: Stack using Linked List ::
***** MENU ****
1. Push
2. Pop
3. Display
4. Exit
Enter your choice: 1
Enter the value to be insert: 10
Insertion is Success!!!
***** MENU *****
1. Push
2. Pop
3. Display
4. Exit
Enter your choice: 1
Enter the value to be insert: 20_
```



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Output

```
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C:\WINDOWS\system32\cmd.exe - tc
4. Exit
Enter your choice: 2
Deleted element: 20
****** MENU *****
1. Push
2. Pop
3. Display
4. Exit
Enter your choice: 3
10--->NULL
***** MENU ****
1. Push
2. Pop
3. Display
4. Exit
Enter your choice: 2
Deleted element: 10
****** MENU *****
1. Push
2. Pop
3. Display
4. Exit
Enter your choice:
```



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Expressions

- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/expressions.html
 - Infix
 - Postfix
 - Prefix



What is an Expression?

- In any programming language, if we want to perform any calculation or to frame a condition etc.,
- we use a set of symbols to perform the task.
- These set of symbols makes an expression.



What is an Expression?

- An expression is a collection of operators and operands that represents a specific value.
- In above definition, **operator** is a symbol which performs a particular task like arithmetic operation or logical operation or conditional operation etc.,
- Operands are the values on which the operators can perform the task. Here operand can be a direct value or variable or address of memory location.



Expression Types

- Based on the operator position, expressions are divided into THREE types. They are as follows...
 - Infix Expression
 - Postfix Expression
 - Prefix Expression



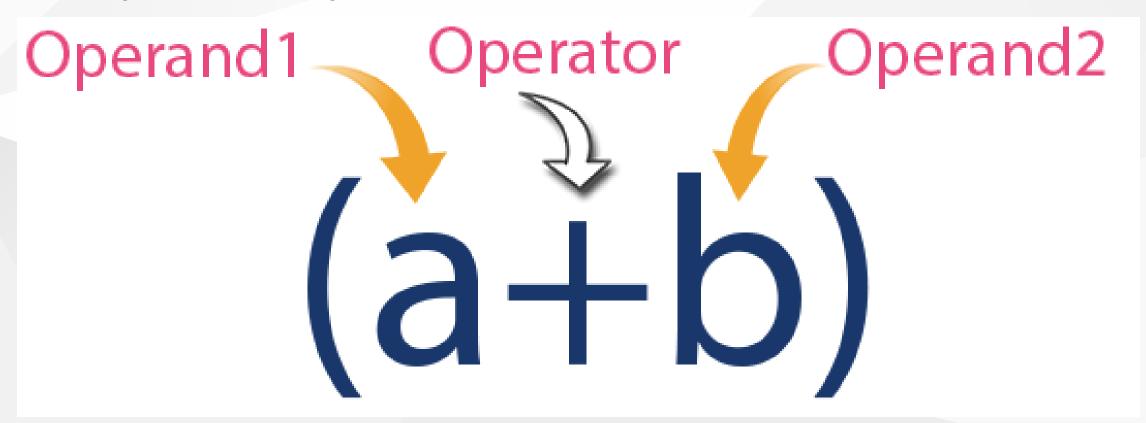
Infix Expression

- In infix expression, operator is used in between the operands.
- The general structure of an Infix expression is as follows.

Operand1 Operator Operand2



Infix Expression Example





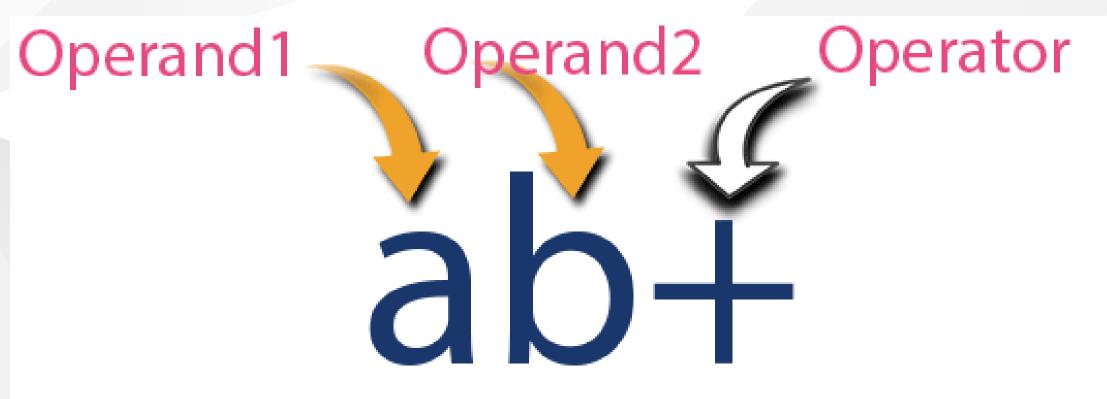
Postfix Expression

- In postfix expression, operator is used after operands.
- We can say that "Operator follows the Operands".
- The general structure of Postfix expression is as follows.

Operand1 Operand2 Operator



Postfix Expression Example





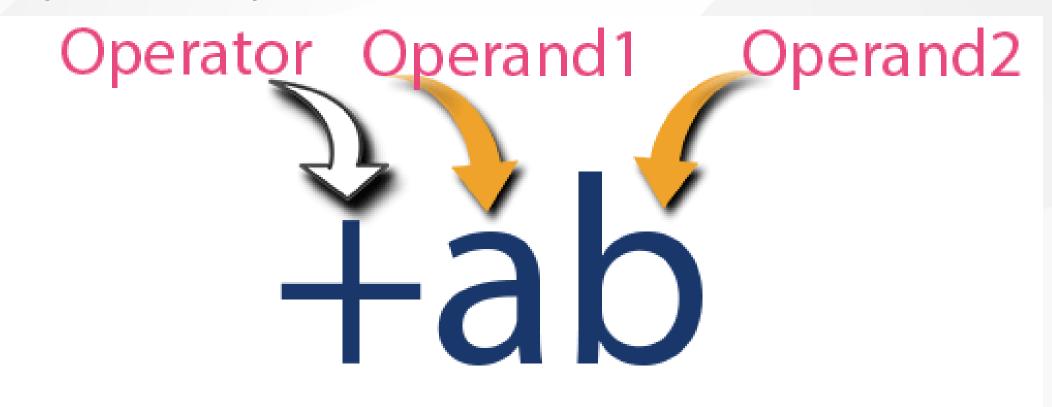
Prefix Expression

- In prefix expression, operator is used before operands.
- We can say that "Operands follows the Operator".
- The general structure of Prefix expression is as follows.

Operator Operand1 Operand2



Prefix Expression Example



• Every expression can be represented using all the above three different types of expressions.



Expression Conversions

- And we can convert an expression from one form to another form like
 - Infix to Postfix,
 - Infix to Prefix,
 - Prefix to Postfix and vice versa.



Infix to Postfix Conversion

- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/infix-to-postfix.html



Infix to Postfix Conversion

- Any expression can be represented using three types of expressions (Infix, Postfix, and Prefix).
- We can also convert one type of expression to another type of expression like
 - Infix to Postfix,
 - Infix to Prefix,
 - Postfix to Prefix and vice versa.



Infix to Postfix Conversion

- To convert any Infix expression into Postfix or Prefix expression we can use the following procedure.
 - o a. Find all the operators in the given Infix Expression.
 - b. Find the order of operators evaluated according to their Operator precedence.
 - c. Convert each operator into required type of expression (Postfix or Prefix)
 in the same order.



Infix to Postfix Example

- Consider the following Infix Expression to be converted into Postfix Expression.
- $\bullet \quad \mathsf{D} = \mathsf{A} + \mathsf{B} * \mathsf{C}$
 - Step 1 The Operators in the given Infix Expression : = , + , *
 - Step 2 The Order of Operators according to their preference: * , + , =
 - Step 3 Now, convert the first operator * -> D = A + B C *
 - Step 4 Convert the next operator + -> D = A BC* +
 - Step 5 Convert the next operator = -> D ABC*+ =
 Finally, given Infix Expression is converted into Postfix Expression as follows...



CE205 Infix to Postfix Conversion using Stack Data Structure

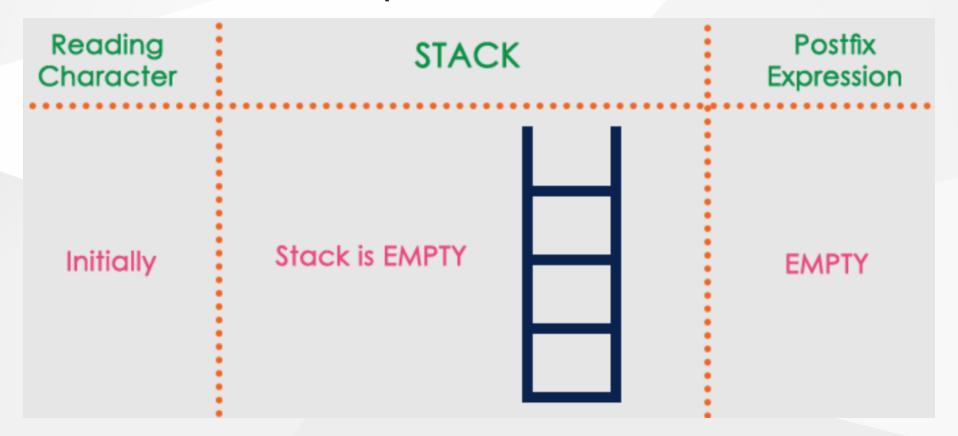
- To convert Infix Expression into Postfix Expression using a stack data structure, We can use the following steps
 - a. Read all the symbols one by one from left to right in the given Infix Expression.
 - b. If the reading symbol is operand, then directly print it to the result (Output).
 - o c. If the reading symbol is left parenthesis '(', then Push it on to the Stack.
 - d. If the reading symbol is right parenthesis ')', then Pop all the contents of stack until respective left parenthesis is poped and print each poped symbol to the result.
 - e. If the reading symbol is operator (+ , , * , / etc.,), then Push it on to the Stack. However, first pop the operators which are already on the stack that have higher or equal precedence than current operator and print them to

the result.

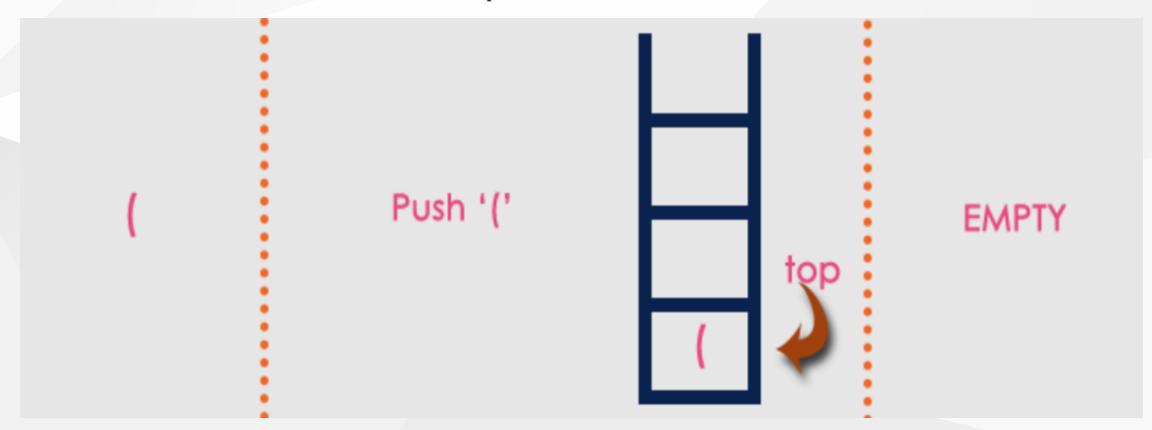
Consider the following Infix Expression...

• The given infix expression can be converted into postfix expression using Stack data Structure as follows.





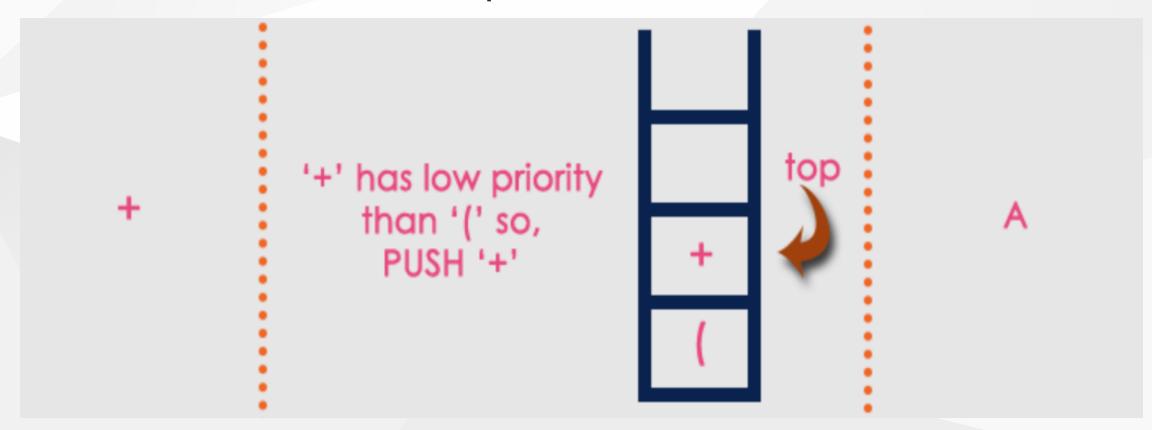








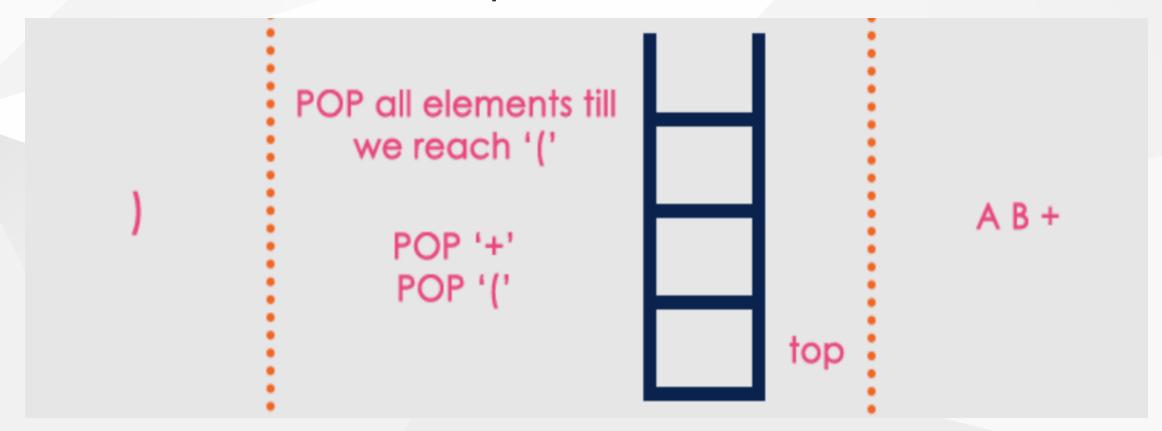








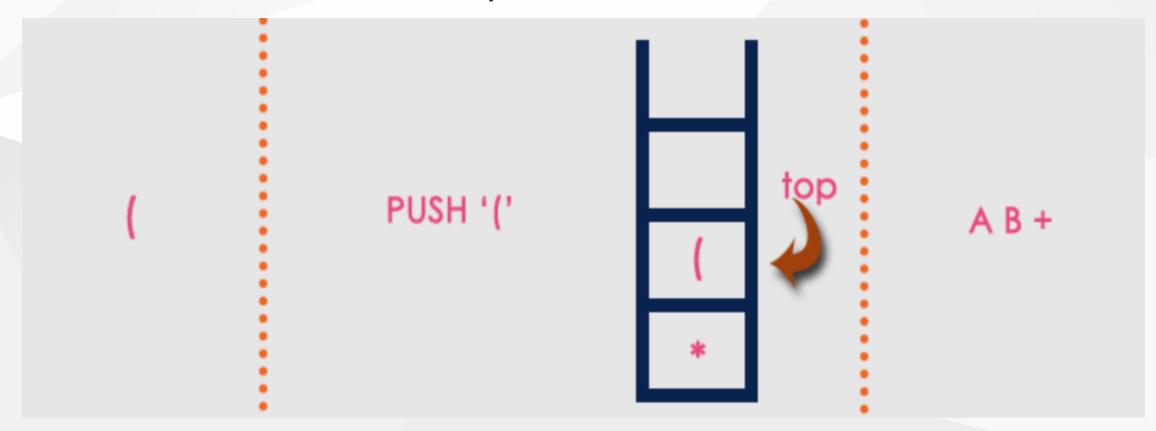








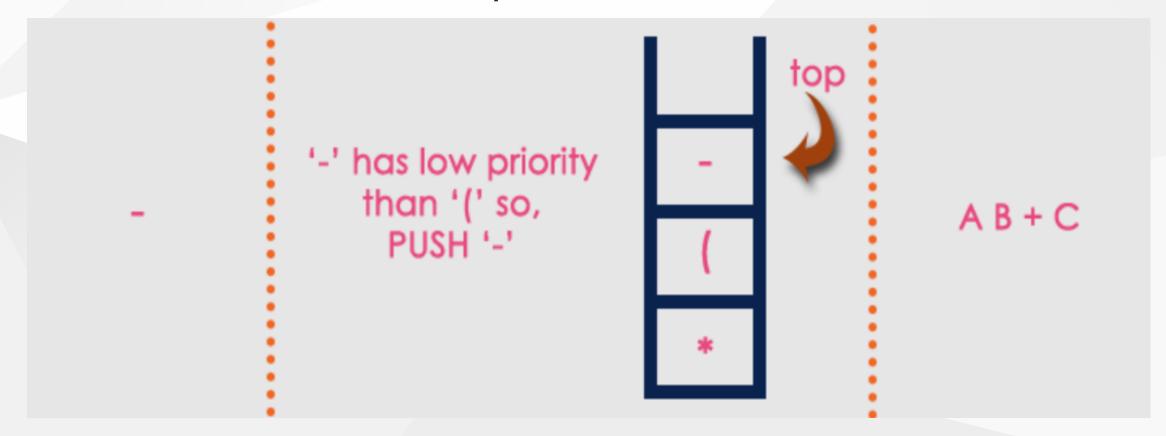


























The final Postfix Expression is as follows...



Postfix Expression Evaluation

- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/postfix-evaluation.html



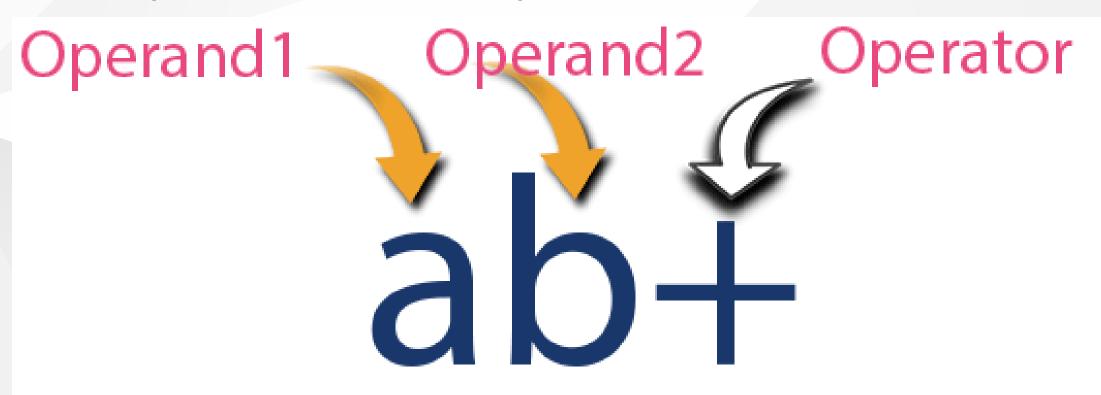
Postfix Expression Evaluation

- A postfix expression is a collection of operators and operands in which the operator is placed after the operands.
- That means, in a postfix expression the operator follows the operands.

Postfix Expression has following general structure

Operand1 Operand2 Operator







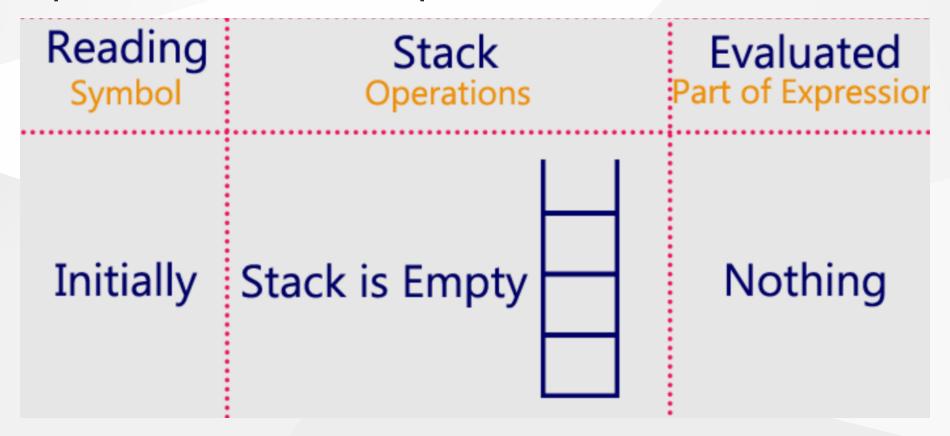
Postfix Expression Evaluation using Stack Data Structure

- A postfix expression can be evaluated using the Stack data structure.
- To evaluate a postfix expression using Stack data structure we can use the following steps
 - a. Read all the symbols one by one from left to right in the given Postfix Expression
 - o b. If the reading symbol is operand, then push it on to the Stack.
 - c. If the reading symbol is operator (+ , , * , / etc.,), then perform TWO pop operations and store the two popped oparands in two different variables (operand1 and operand2). Then perform reading symbol operation using operand1 and operand2 and push result back on to the Stack.
 - d. Finally! perform a pop operation and display the popped value as final result.

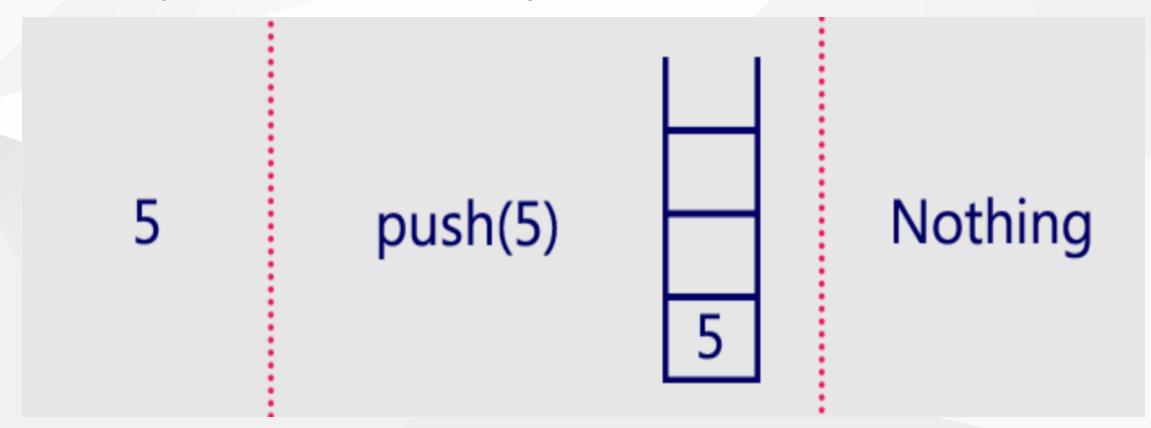
RTEU CE205 Week-3

Consider the following Expression.

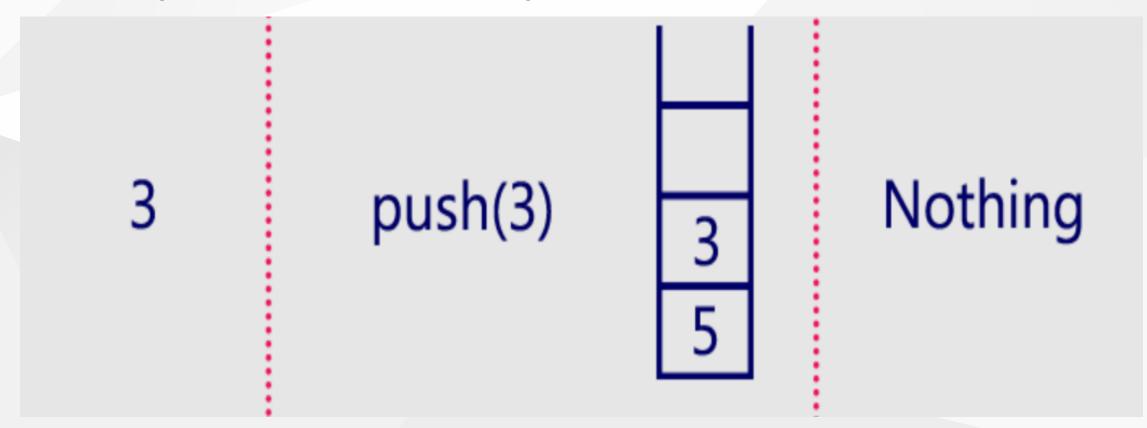
Above Postfix Expression can be evaluated by using Stack Data Structure as follows...



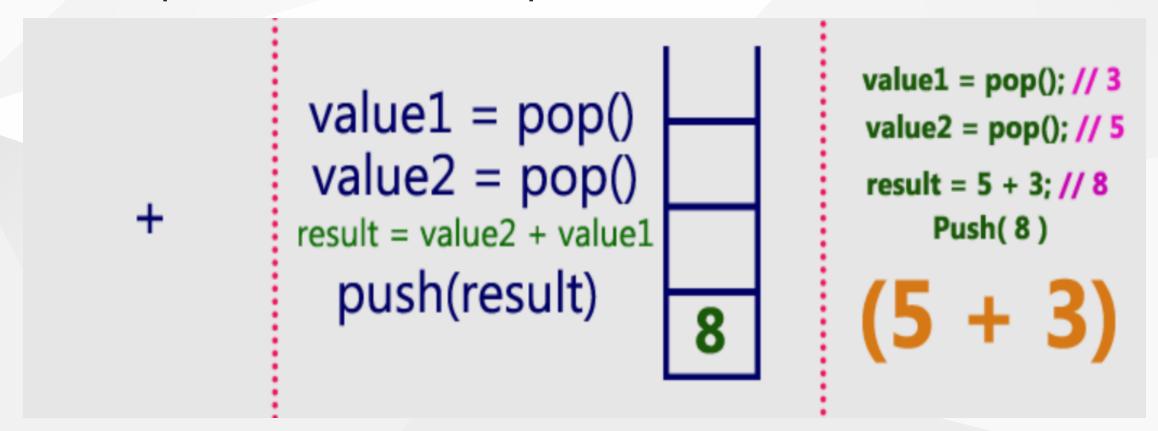




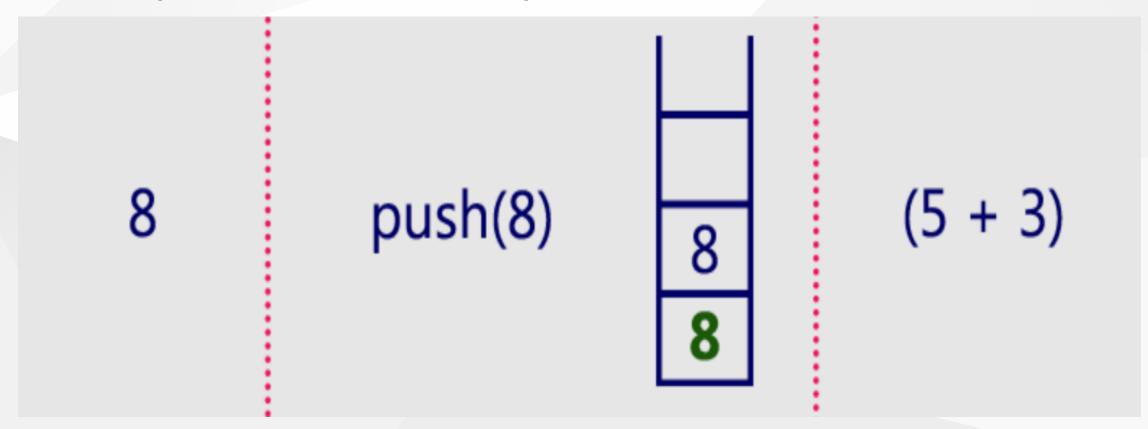




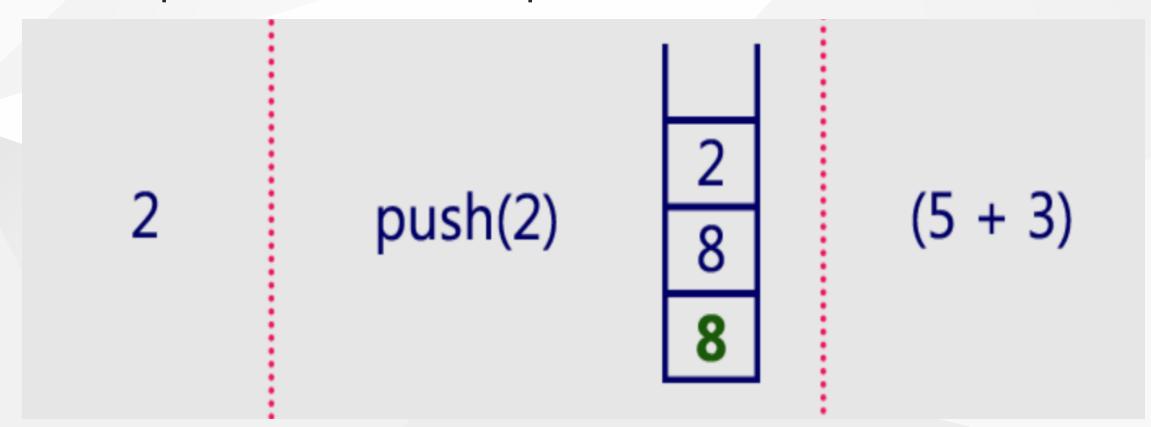


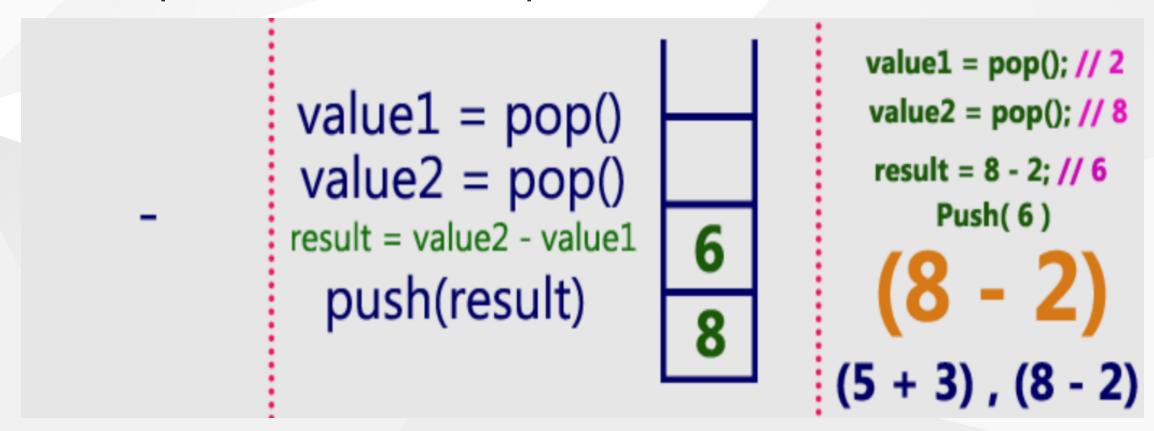




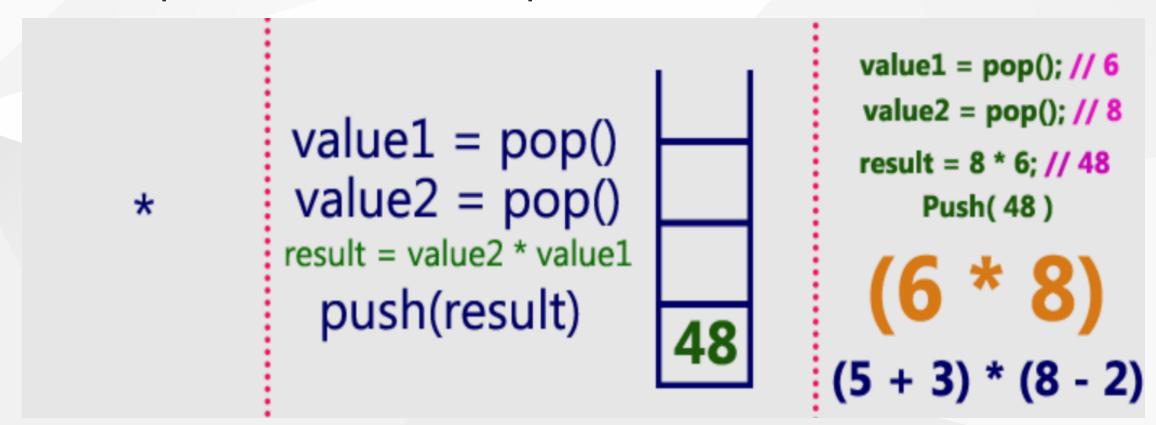


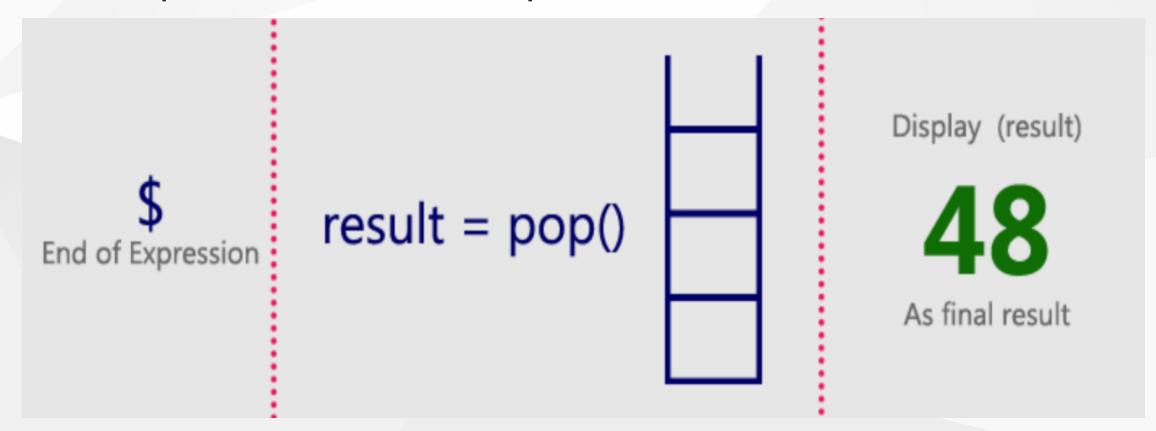












Infix Expression
$$(5 + 3) * (8 - 2) = 48$$

Postfix Expression $5 3 + 8 2 - *$ value is 48



Queue ADT

- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/queue-adt.html



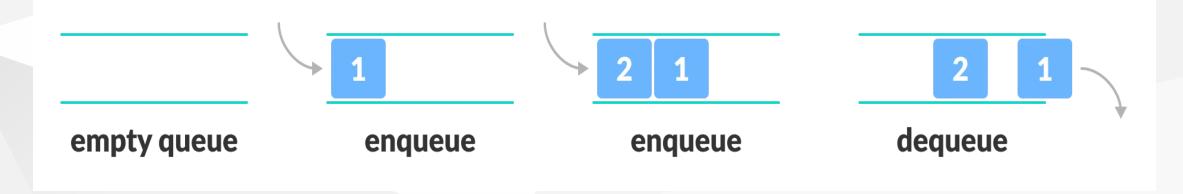
Queue Data Structure

- In this tutorial, you will learn what a queue is. Also, you will find implementation of queue in C, C++, Java and Python.
- A queue is a useful data structure in programming. It is similar to the ticket queue outside a cinema hall, where the first person entering the queue is the first person who gets the ticket.
- Queue follows the **First In First Out (FIFO)** rule the item that goes in first is the item that comes out first.



Queue Data Structure

FIFO Representation of Queue



- In the above image, since 1 was kept in the queue before 2,
- it is the first to be removed from the queue as well.
- It follows the FIFO rule.



Queue Data Structure

- In programming terms, putting items in the queue is called **enqueue**, and removing items from the queue is called **dequeue**.
- We can implement the queue in any programming language like C, C++, Java, Python or C#, but the specification is pretty much the same.



Basic Operations of Queue

- A queue is an object (an abstract data structure ADT) that allows the following operations:
 - Enqueue: Add an element to the end of the queue
 - Dequeue: Remove an element from the front of the queue
 - IsEmpty: Check if the queue is empty
 - IsFull: Check if the queue is full
 - o Peek: Get the value of the front of the queue without removing it



Working of Queue

- Queue operations work as follows:
 - two pointers FRONT and REAR
 - FRONT track the first element of the queue
 - REAR track the last element of the queue
 - o initially, set value of FRONT and REAR to -1



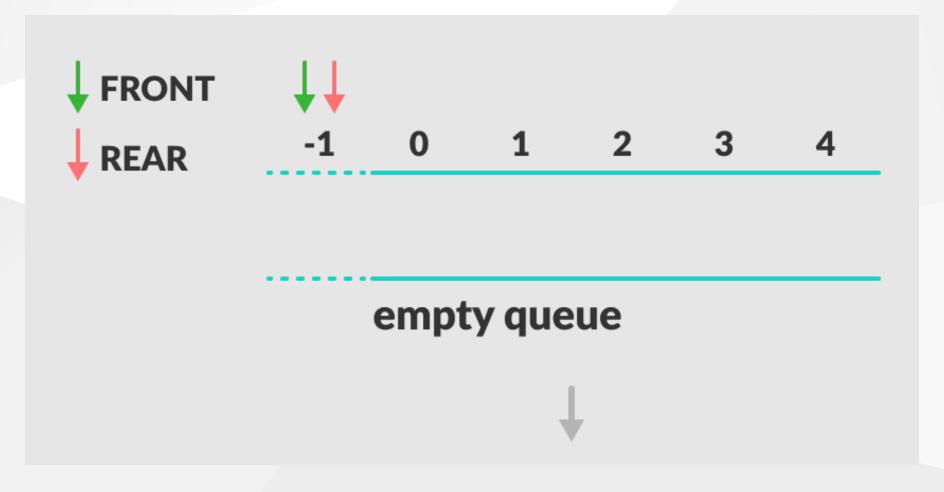
Enqueue Operation

- check if the queue is full
- for the first element, set the value of FRONT to 0
- increase the REAR index by 1
- add the new element in the position pointed to by REAR

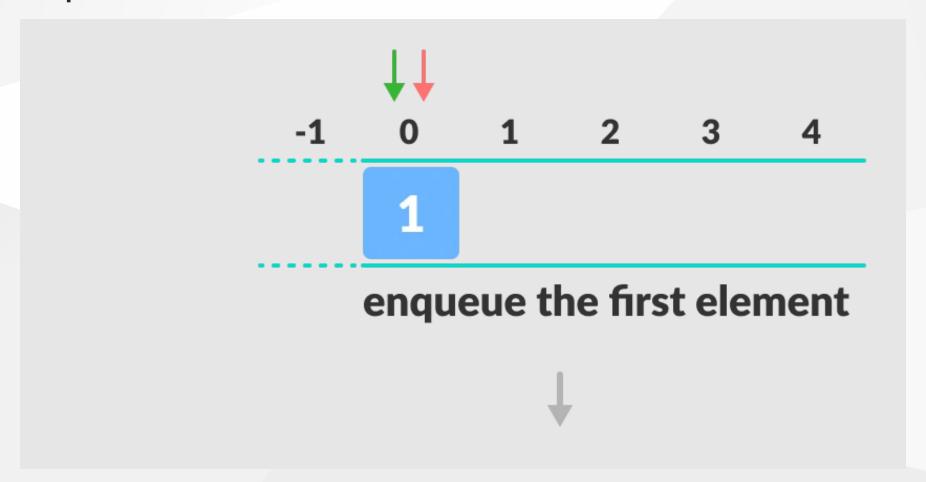


- check if the queue is empty
- return the value pointed by FRONT
- increase the FRONT index by 1
- for the last element, reset the values of FRONT and REAR to -1

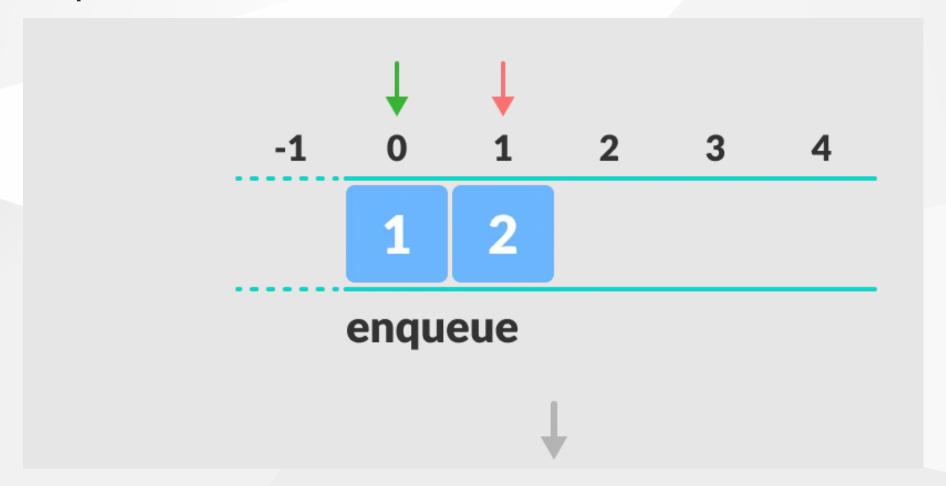




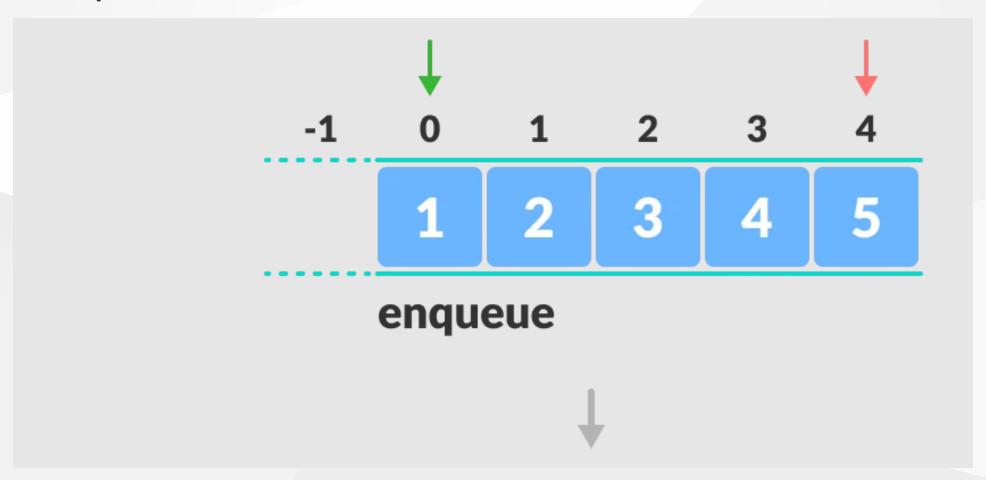




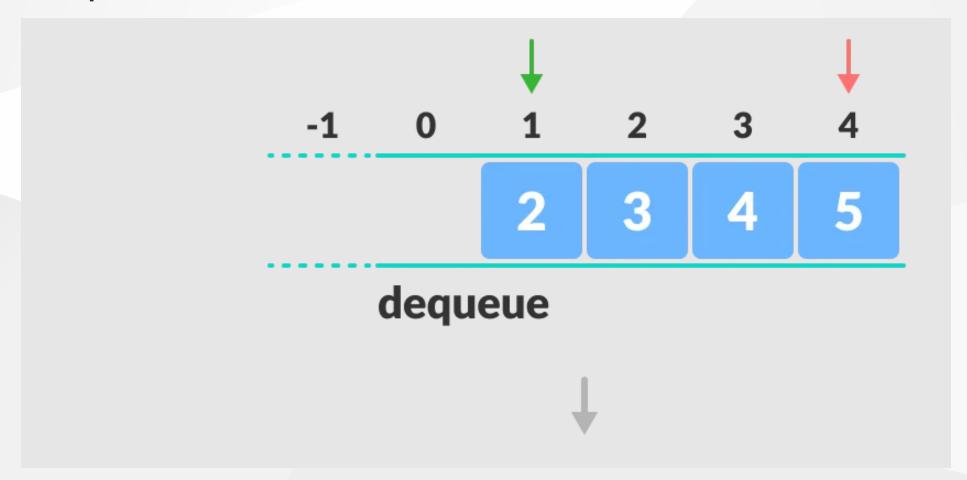




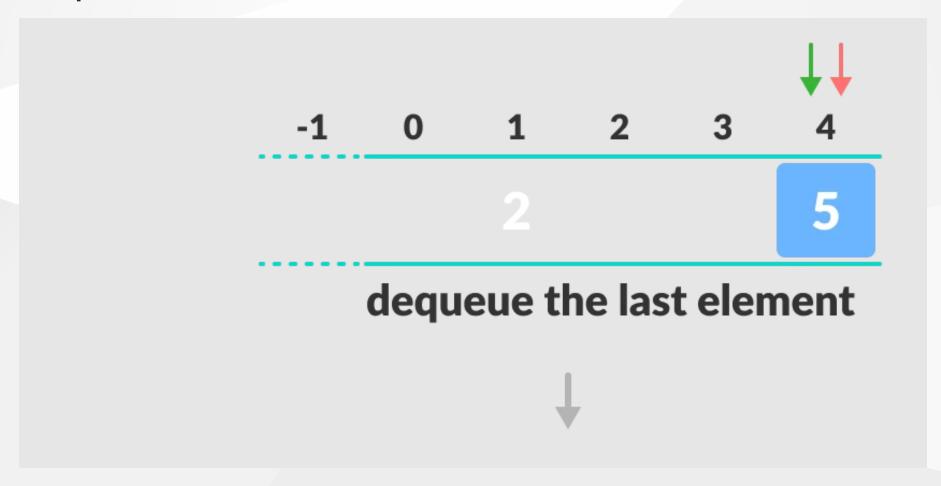




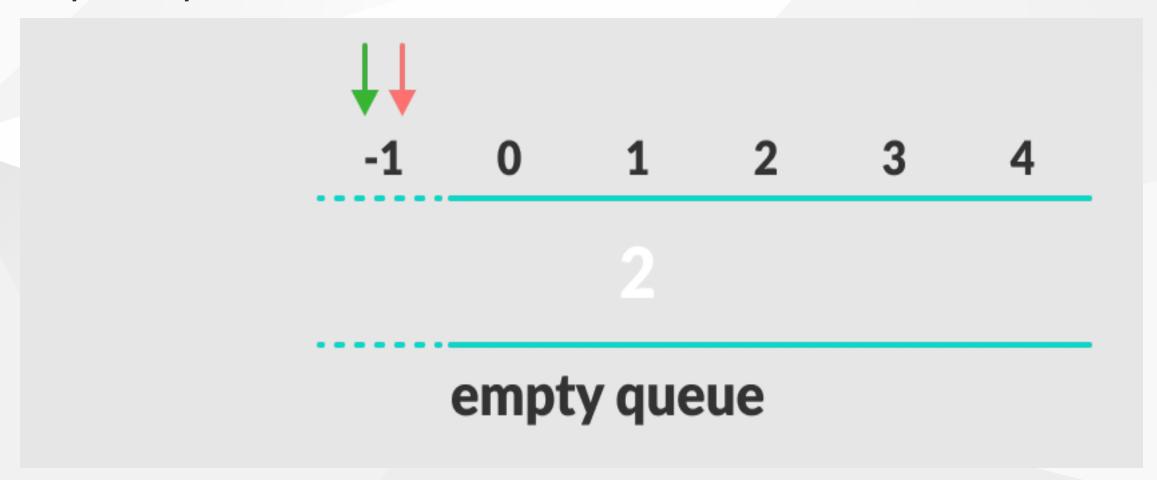
















```
// Queue implementation in C

#include <stdio.h>
#define SIZE 5

void enQueue(int);
void deQueue();
void display();
...
```





```
int items[SIZE], front = -1, rear = -1;
```





```
int main() {
 //deQueue is not possible on empty queue
 deQueue();
  //enQueue 5 elements
  enQueue(1);
  enQueue(2);
  enQueue(3);
  enQueue(4);
  enQueue(5);
 // 6th element can't be added to because the queue is full
  enQueue(6);
 display();
 //deQueue removes element entered first i.e. 1
 deQueue();
 //Now we have just 4 elements
 display();
  return 0;
```





```
void enQueue(int value) {
  if (rear == SIZE - 1)
    printf("\nQueue is Full!!");
  else {
    if (front == -1)
      front = 0;
    rear++;
    items[rear] = value;
    printf("\nInserted -> %d", value);
```





```
void deQueue() {
  if (front == -1)
    printf("\nQueue is Empty!!");
  else {
    printf("\nDeleted : %d", items[front]);
    front++;
    if (front > rear)
      front = rear = -1;
```





```
// Function to print the queue
void display() {
  if (rear == -1)
    printf("\nQueue is Empty!!!");
  else {
    int i;
    printf("\nQueue elements are:\n");
    for (i = front; i <= rear; i++)</pre>
      printf("%d ", items[i]);
  printf("\n");
```





```
// Queue implementation in C++
#include <iostream>
#define SIZE 5
using namespace std;
class Queue {
   private:
  int items[SIZE], front, rear;
   public:
  Queue() {
    front = -1;
    rear = -1;
• • •
```





```
bool isFull() {
   if (front == 0 && rear == SIZE - 1) {
      return true;
   }
   return false;
}
```





```
bool isEmpty() {
   if (front == -1)
     return true;
   else
     return false;
}
...
```





```
void enQueue(int element) {
  if (isFull()) {
    cout << "Queue is full";</pre>
  } else {
    if (front == -1) front = 0;
    rear++;
    items[rear] = element;
    cout << endl</pre>
        << "Inserted " << element << endl;</pre>
```





```
int deQueue() {
   int element;
   if (isEmpty()) {
     cout << "Queue is empty" << endl;</pre>
     return (-1);
   } else {
     element = items[front];
     if (front >= rear) {
       front = -1;
       rear = -1;
     } /* Q has only one element, so we reset the queue after deleting it. */
     else {
        front++;
     cout << endl
        << "Deleted -> " << element << endl;</pre>
     return (element);
. . .
```





```
void display() {
    /* Function to display elements of Queue */
    int i;
    if (isEmpty()) {
       cout << endl</pre>
          << "Empty Queue" << endl;</pre>
    } else {
       cout << endl</pre>
          << "Front index-> " << front;</pre>
       cout << endl
          << "Items -> ";
      for (i = front; i <= rear; i++)</pre>
         cout << items[i] << " ";</pre>
       cout << endl</pre>
          << "Rear index-> " << rear << endl;</pre>
};
. . .
```





```
int main() {
 Queue q;
 //deQueue is not possible on empty queue
  q.deQueue();
  //enQueue 5 elements
  q.enQueue(1);
  q.enQueue(2);
  q.enQueue(3);
  q.enQueue(4);
 q.enQueue(5);
 // 6th element can't be added to because the queue is full
 q.enQueue(6);
  q.display();
 //deQueue removes element entered first i.e. 1
 q.deQueue();
 //Now we have just 4 elements
 q.display();
  return 0;
```



```
// Queue implementation in Java
public class Queue {
  int SIZE = 5;
  int items[] = new int[SIZE];
  int front, rear;
 Queue() {
    front = -1;
    rear = -1;
```

```
boolean isFull() {
   if (front == 0 && rear == SIZE - 1) {
      return true;
   }
   return false;
}
```

```
boolean isEmpty() {
   if (front == -1)
     return true;
   else
     return false;
}
```



```
void enQueue(int element) {
  if (isFull()) {
    System.out.println("Queue is full");
  } else {
    if (front == -1)
      front = 0;
    rear++;
    items[rear] = element;
    System.out.println("Inserted " + element);
```



```
int deQueue() {
   int element;
   if (isEmpty()) {
     System.out.println("Queue is empty");
     return (-1);
   } else {
     element = items[front];
     if (front >= rear) {
       front = -1;
       rear = -1;
     } /* Q has only one element, so we reset the queue after deleting it. */
     else {
       front++;
     System.out.println("Deleted -> " + element);
     return (element);
. . .
```



```
void display() {
  /* Function to display elements of Queue */
  int i;
  if (isEmpty()) {
    System.out.println("Empty Queue");
  } else {
    System.out.println("\nFront index-> " + front);
    System.out.println("Items -> ");
    for (i = front; i <= rear; i++)</pre>
      System.out.print(items[i] + " ");
    System.out.println("\nRear index-> " + rear);
```

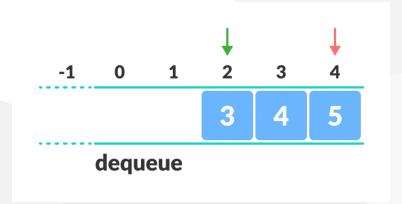
```
public static void main(String[] args) {
  Queue q = new Queue();
  // deQueue is not possible on empty queue
  q.deQueue();
  // enQueue 5 elements
  q.enQueue(1);
  q.enQueue(2);
  q.enQueue(3);
  q.enQueue(4);
  q.enQueue(5);
  // 6th element can't be added to because the queue is full
  q.enQueue(6);
  q.display();
  // deQueue removes element entered first i.e. 1
  q.deQueue();
  // Now we have just 4 elements
  q.display();
```

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Limitations of Queue

• As you can see in the image below, after a bit of enqueuing and dequeuing, the size of the queue has been reduced.





Limitations of Queue

- And we can only add indexes 0 and 1 only when the queue is reset (when all the elements have been dequeued).
- After REAR reaches the last index,
 - o if we can store extra elements in the empty spaces (0 and 1),
 - we can make use of the empty spaces. This is implemented by a modified queue called the circular queue.



Complexity Analysis

- The complexity of enqueue and dequeue operations in a queue using an array is O(1). If you use pop(N) in python code,
- then the complexity might be O(n) depending on the position of the item to be popped.



Applications of Queue

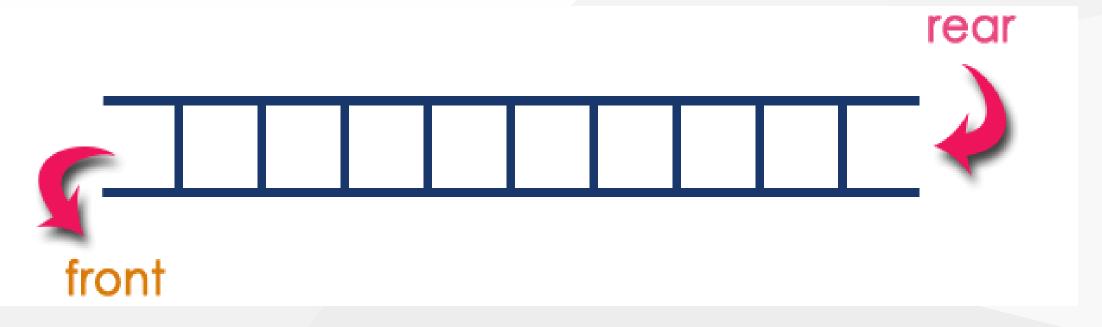
- CPU scheduling, Disk Scheduling
- When data is transferred asynchronously between two processes. The queue is used for synchronization. For example: IO Buffers, pipes, file IO, etc
- Handling of interrupts in real-time systems.
- Call Center phone systems use Queues to hold people calling them in order.



- Queue is a linear data structure in which the insertion and deletion operations are performed at two different ends.
- In a queue data structure, adding and removing elements are performed at two different positions.
- The insertion is performed at one end and deletion is performed at another end. In a queue data structure, the insertion operation is performed at a position which is known as 'rear' and the deletion operation is performed at a position which is known as 'front'.
- In queue data structure, the insertion and deletion operations are performed based on FIFO (First In First Out) principle.



- In a queue data structure,
 - the insertion operation is performed using a function called "enQueue()" and
 - o deletion operation is performed using a function called "deQueue()".

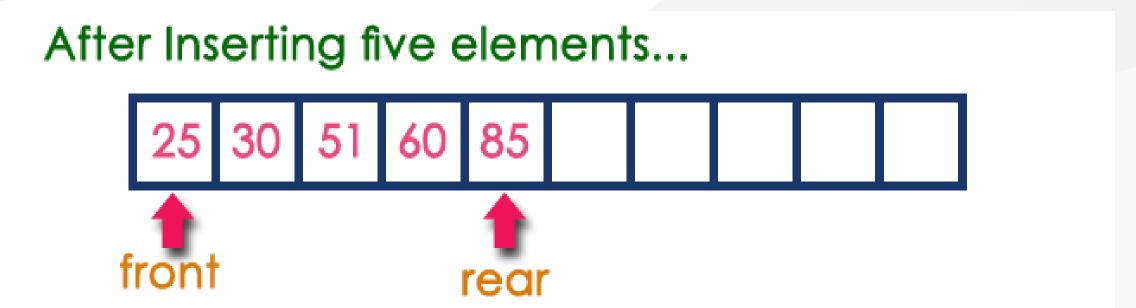




- Queue data structure can be defined as follows.
- Queue data structure is a linear data structure in which the operations are performed based on FIFO principle.
- A queue data structure can also be defined as
- "Queue data structure is a collection of similar data items in which insertion and deletion operations are performed based on FIFO principle".



Queue after inserting 25, 30, 51, 60 and 85.





Operations on a Queue

- The following operations are performed on a queue data structure
 - a. enQueue(value) (To insert an element into the queue)
 - b. deQueue() (To delete an element from the queue)
 - c. display() (To display the elements of the queue)



Queue Implementation

- Queue data structure can be implemented in two ways. They are as follows...
 - o a. Using Array
 - b. Using Linked List
- When a queue is implemented using an array, that queue can organize an only limited number of elements.
- When a queue is implemented using a linked list, that queue can organize an unlimited number of elements.



First Come First Serve, FCFS, FIFO

- BTech Smart Class
 - http://www.btechsmartclass.com/downloads/lab-manuals/Operating-System-Lab-Manual-R18-JNTUH.pdf



Queue Data structure Using Array

- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/queue-using-array.html



Queue Datastructure Using Array

- A queue data structure can be implemented using one dimensional array.
- The queue implemented using array stores only fixed number of data values.
- The implementation of queue data structure using array is very simple.
- Just define a one dimensional array of specific size and insert or delete the values into that array by using FIFO (First In First Out) principle with the help of variables 'front' and 'rear'.



Queue Datastructure Using Array

- Initially both 'front' and 'rear' are set to -1. Whenever, we want to insert a new value into the queue, increment 'rear' value by one and then insert at that position.
- Whenever we want to delete a value from the queue, then delete the element which is at 'front' position and increment 'front' value by one.



CE205 Queue Operations using Array

CE205 Wequeue.

- Queue data structure using array can be implemented as follows.
- Before we implement actual operations, first follow the below steps to create an empty queue.
 - Step 1 Include all the header files which are used in the program and define a constant 'SIZE' with specific value.
 - Step 2 Declare all the user defined functions which are used in queue implementation.
 - Step 3 Create a one dimensional array with above defined SIZE (int queue[SIZE])
 - Step 4 Define two integer variables 'front' and 'rear' and initialize both with '-1'. (int front = -1, rear = -1)
 - Step 5 Then implement main method by displaying menu of operations list and make suitable function calls to perform operation selected by the user on

Queue Operations using Array

enQueue(value) - Inserting value into the queue

- In a queue data structure, enQueue() is a function used to insert a new element into the queue.
- In a queue, the new element is always inserted at rear position.
- The enQueue() function takes one integer value as a parameter and inserts that value into the queue. We can use the following steps to insert an element into the queue
 - Step 1 Check whether queue is FULL. (rear == SIZE-1)
 - Step 2 If it is FULL, then display "Queue is FULL!!! Insertion is not possible!!!" and terminate the function.
 - Step 3 If it is NOT FULL, then increment rear value by one (rear++) and set queue[rear] = value.

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CE205 Queue Operations using Array

deQueue() - Deleting a value from the Queue

- In a queue data structure, deQueue() is a function used to delete an element from the queue.
- In a queue, the element is always deleted from front position.
- The deQueue() function does not take any value as parameter.
- We can use the following steps to delete an element from the queue.
 - Step 1 Check whether queue is EMPTY. (front == rear)
 - Step 2 If it is EMPTY, then display "Queue is EMPTY!!! Deletion is not possible!!!" and terminate the function.
 - Step 3 If it is NOT EMPTY, then increment the front value by one (front ++).
 Then display queue[front] as deleted element. Then check whether both front and rear are equal (front == rear), if it TRUE, then set
 We both front and rear to '-1' (front = rear = -1).

Queue Operations using Array

display() - Displays the elements of a Queue

- -We can use the following steps to display the elements of a queue...
 - Step 1 Check whether queue is EMPTY. (front == rear)
 - Step 2 If it is **EMPTY**, then display "Queue is **EMPTY**!!!" and terminate the function.
 - Step 3 If it is **NOT EMPTY**, then define an integer variable 'i' and set 'i = **front+1**'.
 - Step 4 Display 'queue[i]' value and increment 'i' value by one (i++). Repeat the same until 'i' value reaches to rear (i <= rear)



```
#include<stdio.h>
#include<conio.h>
#define SIZE 10

void enQueue(int);
void deQueue();
void display();
...
```



```
int queue[SIZE], front = -1, rear = -1;
...
```

```
void main()
   int value, choice;
   clrscr();
   while(1){
      printf("\n\n***** MENU *****\n");
      printf("1. Insertion\n2. Deletion\n3. Display\n4. Exit");
      printf("\nEnter your choice: ");
      scanf("%d",&choice);
     switch(choice){
     case 1: printf("Enter the value to be insert: ");
         scanf("%d",&value);
         enQueue(value);
         break;
     case 2: deQueue();
         break;
     case 3: display();
         break;
     case 4: exit(0);
     default: printf("\nWrong selection!!! Try again!!!");
. . .
```

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```
. . .
void enQueue(int value){
   if(rear == SIZE-1)
      printf("\nQueue is Full!!! Insertion is not possible!!!");
   else{
      if(front == -1)
     front = 0;
      rear++;
      queue[rear] = value;
      printf("\nInsertion success!!!");
```

```
void deQueue(){
   if(front == rear)
      printf("\nQueue is Empty!!! Deletion is not possible!!!");
   else{
      printf("\nDeleted : %d", queue[front]);
      front++;
      if(front == rear)
     front = rear = -1;
```

```
void display(){
   if(rear == -1)
      printf("\nQueue is Empty!!!");
   else{
      int i;
      printf("\nQueue elements are:\n");
      for(i=front; i<=rear; i++)</pre>
      printf("%d\t",queue[i]);
```

Output

center h:400px



Queue Using Linked List

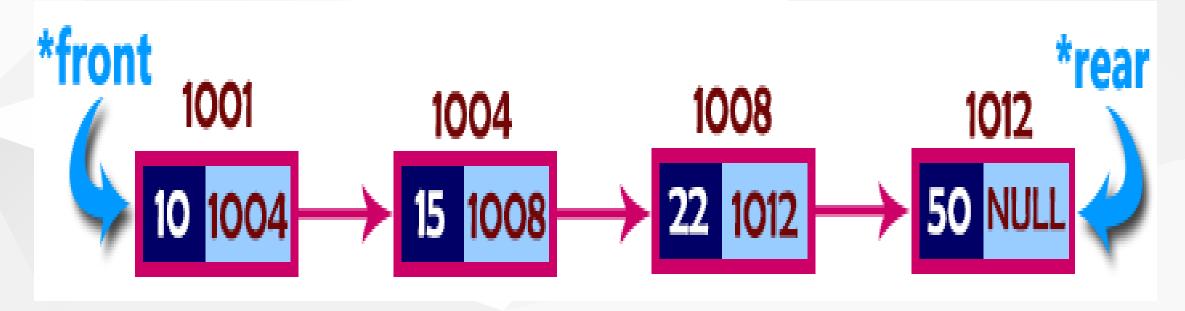
- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/queue-using-linked-list.html



CE205 Queue Using Linked List

- The major problem with the queue implemented using an array is,
- It will work for an only fixed number of data values.
- That means, the amount of data must be specified at the beginning itself.
- Queue using an array is not suitable when we don't know the size of data which we are going to use.
- A queue data structure can be implemented using a linked list data structure. The queue which is implemented using a linked list can work for an unlimited number of values.
- That means, queue using linked list can work for the variable size of data (No need to fix the size at the beginning of the implementation).
- The Queue implemented using linked list can organize as many data values as we want.
- In linked list implementation of a queue, the last inserted node is always pointed by 'front'.

Queue Using Linked List Example



• In above example, the last inserted node is 50 and it is pointed by 'rear' and the first inserted node is 10 and it is pointed by 'front'. The order of elements inserted is 10, 15, 22 and 50.



Operations

- To implement queue using linked list, we need to set the following things before implementing actual operations.
 - Step 1 Include all the header files which are used in the program. And declare all the user defined functions.
 - Step 2 Define a 'Node' structure with two members data and next.
 - Step 3 Define two Node pointers 'front' and 'rear' and set both to NULL.
 - Step 4 Implement the main method by displaying Menu of list of operations and make suitable function calls in the main method to perform user selected operation.



enQueue(value) - Inserting an element into the Queue

- We can use the following steps to insert a new node into the queue...
 - Step 1 Create a newNode with given value and set 'newNode → next' to NULL.
 - Step 2 Check whether queue is Empty (rear == NULL)
 - Step 3 If it is Empty then, set front = newNode and rear = newNode.
 - Step 4 If it is Not Empty then, set rear →
 next = newNode and rear = newNode.



deQueue() - Deleting an Element from Queue

- We can use the following steps to delete a node from the queue...
 - Step 1 Check whether queue is Empty (front == NULL).
 - Step 2 If it is Empty, then display "Queue is Empty!!! Deletion is not possible!!!" and terminate from the function
 - Step 3 If it is Not Empty then, define a Node pointer 'temp' and set it to 'front'.
 - Step 4 Then set 'front = front → next' and delete 'temp' (free(temp)).



display() - Displaying the elements of Queue

- We can use the following steps to display the elements (nodes) of a queue...
 - Step 1 Check whether queue is Empty (front == NULL).
 - Step 2 If it is Empty then, display 'Queue is Empty!!!' and terminate the function.
 - Step 3 If it is **Not Empty** then, define a Node pointer 'temp' and initialize with front.
 - Step 4 Display 'temp → data --->' and move it to the next node. Repeat the same until 'temp' reaches to 'rear' (temp → next != NULL).
 - Step 5 Finally! Display 'temp → data ---> NULL'.



```
#include<stdio.h>
#include<conio.h>

struct Node
{
   int data;
   struct Node *next;
}*front = NULL, *rear = NULL;
...
```

```
void insert(int);
void delete();
void display();
...
```



```
void main()
   int choice, value;
   clrscr();
   printf("\n:: Queue Implementation using Linked List ::\n");
   while(1){
      printf("\n***** MENU *****\n");
      printf("1. Insert\n2. Delete\n3. Display\n4. Exit\n");
      printf("Enter your choice: ");
      scanf("%d",&choice);
      switch(choice){
     case 1: printf("Enter the value to be insert: ");
         scanf("%d", &value);
         insert(value);
         break;
     case 2: delete(); break;
     case 3: display(); break;
     case 4: exit(0);
     default: printf("\nWrong selection!!! Please try again!!!\n");
. . .
```

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```
void insert(int value)
   struct Node *newNode;
   newNode = (struct Node*)malloc(sizeof(struct Node));
   newNode->data = value;
   newNode -> next = NULL;
   if(front == NULL)
      front = rear = newNode;
   else{
      rear -> next = newNode;
      rear = newNode;
   printf("\nInsertion is Success!!!\n");
. . .
```

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```
void delete()
   if(front == NULL)
      printf("\nQueue is Empty!!!\n");
   else{
      struct Node *temp = front;
      front = front -> next;
      printf("\nDeleted element: %d\n", temp->data);
      free(temp);
```

```
void display()
   if(front == NULL)
      printf("\nQueue is Empty!!!\n");
   else{
      struct Node *temp = front;
      while(temp->next != NULL){
     printf("%d--->",temp->data);
     temp = temp -> next;
      printf("%d--->NULL\n",temp->data);
```

Output

```
:: Queue Implementation using Linked List ::

******* MENU *******

1. Insert
2. Delete
3. Display
4. Exit
Enter your choice: 1
Enter the value to be insert: 10

Insertion is Success!!!

******** MENU *******

1. Insert
2. Delete
3. Display
4. Exit
Enter your choice: 1
Enter the value to be insert: 20

Insertion is Success!!!
```



Output

```
C:\WINDOWS\system32\cmd.exe - tc

10--->20--->NULL

******** MENU ********

1. Insert

2. Delete

3. Display

4. Exit
Enter your choice: 2

Deleted element: 10

******** MENU *******

1. Insert

2. Delete

3. Display

4. Exit
Enter your choice: 3

20--->NULL

******** MENU *******

1. Insert

2. Delete

3. Display

4. Exit
Enter your choice: 3

20--->NULL

********* MENU *******

1. Insert

2. Delete

3. Display

4. Exit
Enter your choice: _______
```

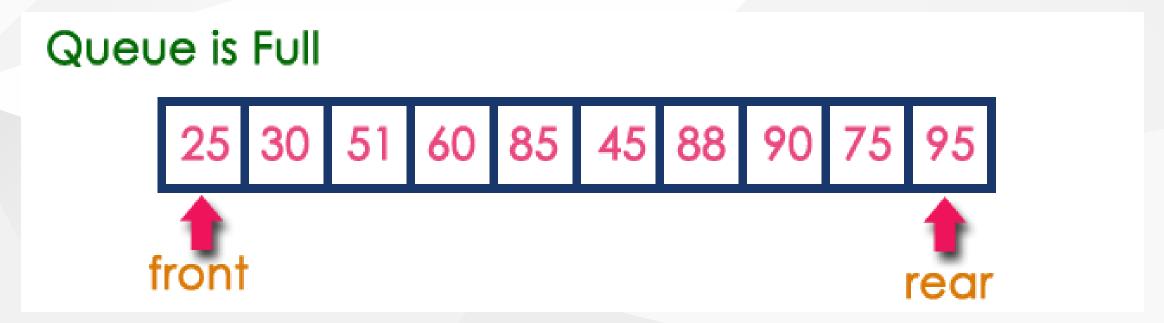


- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/circular-queue.html



- In a normal Queue Data Structure, we can insert elements until queue becomes full.
- But once the queue becomes full, we can not insert the next element until all the elements are deleted from the queue.
- For example, consider the queue below.
- The queue after inserting all the elements into it is as follows...





• Now consider the following situation after deleting three elements from the queue.



Queue is Full (Even three elements are deleted)





- This situation also says that Queue is Full and we cannot insert the new element because 'rear' is still at last position.
- In the above situation, even though we have empty positions in the queue we can not make use of them to insert the new element.
- This is the major problem in a normal queue data structure.
- To overcome this problem we use a circular queue data structure.



What is Circular Queue?

- A Circular Queue can be defined as follows.
- A circular queue is a linear data structure in which the operations are performed based on FIFO (First In First Out) principle and the last position is connected back to the first position to make a circle.
- Graphical representation of a circular queue is as follows.

![center h:300px](assets/Circular Q.png)



Implementation of Circular Queue

To implement a circular queue data structure using an array, we first perform the following steps before we implement actual operations.

- Step 1 Include all the **header files** which are used in the program and define a constant 'SIZE' with specific value.
- Step 2 Declare all user defined functions used in circular queue implementation.
- Step 3 Create a one dimensional array with above defined SIZE (int cQueue[SIZE])
- Step 4 Define two integer variables 'front' and 'rear' and initialize both with '-1'. (int front = -1, rear = -1)
- Step 5 Implement main method by displaying menu of operations list and make suitable function calls to perform operation selected by the user on circular queue.



enQueue(value) - Inserting value into the Circular Queue

In a circular queue, enQueue() is a function which is used to insert an element into the circular queue. In a circular queue, the new element is always inserted at **rear** position. The enQueue() function takes one integer value as parameter and inserts that value into the circular queue. We can use the following steps to insert an element into the circular queue...



enQueue(value) - Inserting value into the Circular Queue

- Step 1 Check whether queue is FULL. ((rear == SIZE-1 && front == 0) || (front == rear+1))
- Step 2 If it is **FULL**, then display "Queue is **FULL**!!! **Insertion is not possible**!!!" and terminate the function.
- Step 3 If it is NOT FULL, then check rear == SIZE 1 && front != 0 if it is TRUE, then set rear = -1.
- Step 4 Increment rear value by one (rear++), set queue[rear] = value and check 'front == -1' if it is TRUE, then set front = 0.



deQueue() - Deleting a value from the Circular Queue

In a circular queue, deQueue() is a function used to delete an element from the circular queue. In a circular queue, the element is always deleted from **front** position. The deQueue() function doesn't take any value as a parameter. We can use the following steps to delete an element from the circular queue.



deQueue() - Deleting a value from the Circular Queue

- Step 1 Check whether queue is EMPTY. (front == -1 && rear == -1)
- Step 2 If it is **EMPTY**, then display "Queue is **EMPTY!!! Deletion is not possible!!!**" and terminate the function.
- Step 3 If it is **NOT EMPTY**, then display **queue[front]** as deleted element and increment the **front** value by one (**front** ++). Then check whether **front** == **SIZE**, if it is **TRUE**, then set **front** = **0**. Then check whether both **front 1** and **rear** are equal (**front** -**1** == **rear**), if it **TRUE**, then set both **front** and **rear** to '-**1**' (**front** = **rear** = -**1**).



CE205 display() 4 Displays the elements of a Circular Queue

We can use the following steps to display the elements of a circular queue...

- Step 1 Check whether queue is EMPTY. (front == -1)
- Step 2 If it is **EMPTY**, then display "Queue is **EMPTY**!!!" and terminate the function.
- Step 3 If it is **NOT EMPTY**, then define an integer variable 'i' and set 'i = front'.
- Step 4 Check whether 'front <= rear', if it is TRUE, then display 'queue[i]' value and increment 'i' value by one (i++). Repeat the same until 'i <= rear' becomes FALSE.
- Step 5 If 'front <= rear' is FALSE, then display 'queue[i]' value and increment 'i' value by one (i++). Repeat the same until'i <= SIZE 1' becomes FALSE.
- Step 6 Set i to **0**.
- Step 7 Again display 'cQueue[i]' value and increment i value by one (i++). Repeat ucthesame until 'i <= rear' becomes FALSE.

```
#include<stdio.h>
#include<conio.h>
#define SIZE 5
...
```



```
void enQueue(int);
void deQueue();
void display();
...
```



```
int cQueue[SIZE], front = -1, rear = -1;
...
```



```
. . .
void main()
   int choice, value;
   clrscr();
   while(1){
      printf("\n***** MENU *****\n");
      printf("1. Insert\n2. Delete\n3. Display\n4. Exit\n");
      printf("Enter your choice: ");
      scanf("%d",&choice);
      switch(choice){
     case 1: printf("\nEnter the value to be insert: ");
         scanf("%d",&value);
         enQueue(value);
         break;
     case 2: deQueue();
         break;
     case 3: display();
         break;
     case 4: exit(0);
     default: printf("\nPlease select the correct choice!!!\n");
```



```
void enQueue(int value)
   if((front == 0 && rear == SIZE - 1) || (front == rear+1))
      printf("\nCircular Queue is Full! Insertion not possible!!!\n");
   else{
      if(rear == SIZE-1 && front != 0)
     rear = -1;
      cQueue[++rear] = value;
      printf("\nInsertion Success!!!\n");
      if(front == -1)
     front = 0;
```

```
. . .
void deQueue()
   if(front == -1 && rear == -1)
      printf("\nCircular Queue is Empty! Deletion is not possible!!!\n");
   else{
      printf("\nDeleted element : %d\n",cQueue[front++]);
      if(front == SIZE)
     front = 0;
      if(front-1 == rear)
     front = rear = -1;
```

```
. . .
void display()
   if(front == -1)
      printf("\nCircular Queue is Empty!!!\n");
   else{
      int i = front;
      printf("\nCircular Queue Elements are : \n");
      if(front <= rear){</pre>
     while(i <= rear)</pre>
        printf("%d\t",cQueue[i++]);
      else{
     while(i <= SIZE - 1)</pre>
         printf("%d\t", cQueue[i++]);
     i = 0;
     while(i <= rear)</pre>
         printf("%d\t",cQueue[i++]);
```

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Output

```
_ 🗆 🗙
 C:\WINDOWS\system32\cmd.exe - tc
1. Insert
2. Delete
3. Display
4. Exit
Enter your choice: 1
Enter the value to be insert: 30
Insertion Success!!!
***** MENU *****
1. Insert
2. Delete
3. Display
4. Exit
Enter your choice: 3
Circular Queue Elements are :
10 20 30
****** MENU ******
1. Insert
2. Delete
3. Display
4. Exit
Enter your choice:
```



Output

```
_ 🗆 🗙
 C:\WINDOWS\system32\cmd.exe - tc
***** MENU *****
1. Insert
2. Delete
3. Display
4. Exit
Enter your choice: 2
Deleted element : 20
***** MENU *****
1. Insert
2. Delete
3. Display
4. Exit
Enter your choice: 3
Circular Queue Elements are :
***** MENU *****
1. Insert
2. Delete
3. Display
4. Exit
Enter your choice:
```



Double Ended Queue Data structure

- BTech Smart Class
 - http://www.btechsmartclass.com/data_structures/double-ended-queue.html

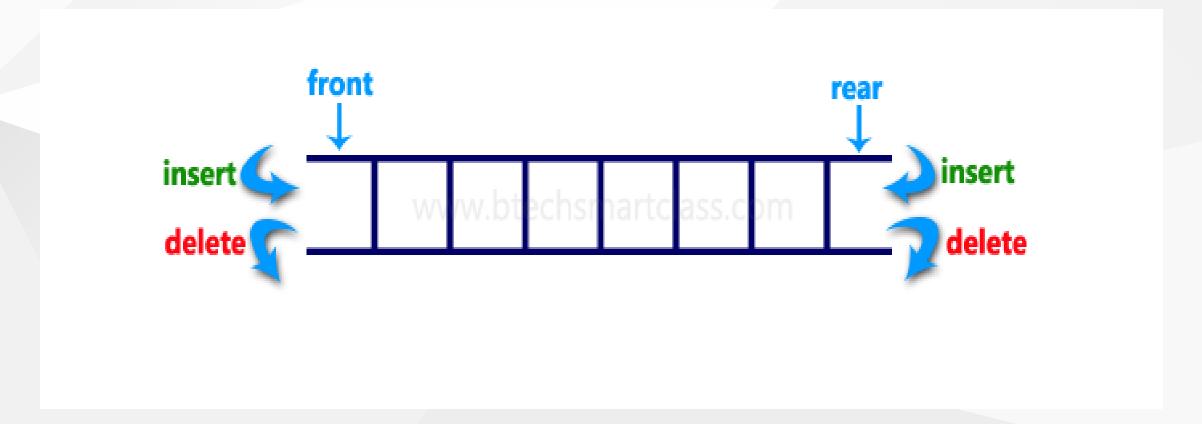


Double Ended Queue Datastructure

- Double Ended Queue is also a Queue data structure in which the insertion and deletion operations are performed at
 - o both the ends (front and rear).
- That means, we can insert at both front and rear positions and can delete from both front and rear positions.



Double Ended Queue Datastructure





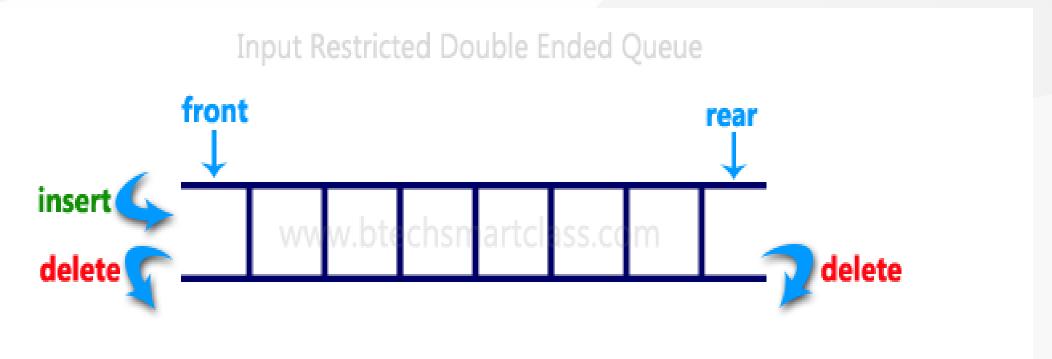
Double Ended Queue Datastructure

- Double Ended Queue can be represented in TWO ways, those are as follows.
 - a. Input Restricted Double Ended Queue
 - b. Output Restricted Double Ended Queue



Input Restricted Double Ended Queue

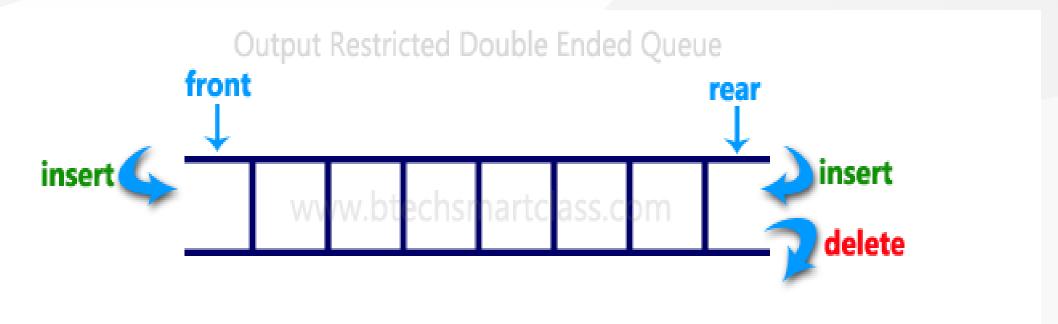
• In input restricted double-ended queue, the insertion operation is performed at only one end and deletion operation is performed at both the ends.





Output Restricted Double Ended Queue

In output restricted double ended queue, the deletion operation is performed at only one end and insertion operation is performed at both the ends.





```
#include<stdio.h>
#include<conio.h>
#define SIZE 100
void enQueue(int);
int deQueueFront();
int deQueueRear();
void enQueueRear(int);
void enQueueFront(int);
void display();
```



```
int queue[SIZE];
int rear = 0, front = 0;
...
```



```
int main()
    char ch;
    int choice1, choice2, value;
    printf("\n****** Type of Double Ended Queue ******\n");
     do
          printf("\n1.Input-restricted deque \n");
          printf("2.output-restricted deque \n");
          printf("\nEnter your choice of Queue Type : ");
          scanf("%d",&choice1);
          switch(choice1)
. . .
```

```
case 1:
    printf("\nSelect the Operation\n");
    printf("1.Insert\n2.Delete from Rear\n3.Delete from Front\n4. Display");
        printf("\nEnter your choice for the operation in c deque: ");
        scanf("%d",&choice2);
        switch(choice2)
          case 1: enQueueRear(value);
                   display();
                  break;
              case 2: value = deQueueRear();
                  printf("\nThe value deleted is %d",value);
                  display();
                  break;
          case 3: value=deQueueFront();
                      printf("\nThe value deleted is %d",value);
                   display();
                      break;
          case 4: display();
                   break;
          default:printf("Wrong choice");
        printf("\nDo you want to perform another operation (Y/N): ");
        ch=getch();
    }while(ch=='y'||ch=='Y');
    getch();
    break;
```

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```
case 2:
            printf("\n---- Select the Operation ----\n");
            printf("1. Insert at Rear\n2. Insert at Front\n3. Delete\n4. Display");
               printf("\nEnter your choice for the operation: ");
               scanf("%d",&choice2);
                switch(choice2)
                  case 1: enQueueRear(value);
                          display();
                          break;
                  case 2: enQueueFront(value);
                          display();
                          break;
                  case 3: value = deQueueFront();
                          printf("\nThe value deleted is %d",value);
                          display();
                          break;
                  case 4: display();
                          break;
                  default:printf("Wrong choice");
                printf("\nDo you want to perform another operation (Y/N): ");
                 ch=getch();
             } while(ch=='y'||ch=='Y');
             getch();
             break ;
     printf("\nDo you want to continue(y/n):");
     ch=getch();
}while(ch=='y'||ch=='Y');
```

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```
. . .
void enQueueRear(int value)
     char ch;
     if(front == SIZE/2)
            printf("\nQueue is full!!! Insertion is not possible!!! ");
            return;
      do
            printf("\nEnter the value to be inserted:");
            scanf("%d",&value);
            queue[front] = value;
            front++;
            printf("Do you want to continue insertion Y/N");
            ch=getch();
      }while(ch=='y');
. . .
```



```
. . .
void enQueueFront(int value)
     char ch;
     if(front==SIZE/2)
            printf("\nQueue is full!!! Insertion is not possible!!!");
            return;
      do
            printf("\nEnter the value to be inserted:");
            scanf("%d",&value);
            rear--;
            queue[rear] = value;
            printf("Do you want to continue insertion Y/N");
            ch = getch();
      while(ch == 'y');
```

```
• • •
int deQueueRear()
     int deleted;
     if(front == rear)
            printf("\nQueue is Empty!!! Deletion is not possible!!!");
            return 0;
     front--;
     deleted = queue[front+1];
     return deleted;
```

```
• • •
int deQueueFront()
     int deleted;
     if(front == rear)
            printf("\nQueue is Empty!!! Deletion is not possible!!!");
            return 0;
     rear++;
     deleted = queue[rear-1];
     return deleted;
```

```
void display()
     int i;
     if(front == rear)
        printf("\nQueue is Empty!!! Deletion is not possible!!!");
     else{
        printf("\nThe Queue elements are:");
        for(i=rear; i < front; i++)</pre>
           printf("%d\t ",queue[i]);
```

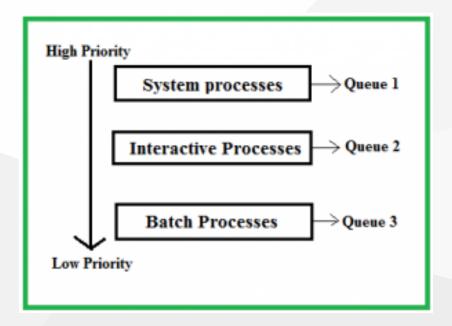
Output

```
III "C:\Users\User\Desktop\New folder\DoubleEndedQueue\bin\Debug\DoubleEndedQueue.exe"
                                                                                                                  ****** Type of Double Ended Queue ******
1.Input-restricted deque
output-restricted deque
Enter your choice of Queue Type : 1
Select the Operation
1.Insert
2.Delete from Rear
 3.Delete from Front
 1. Display
Enter your choice for the operation in c deque: 1
Enter the value to be inserted:10
Do you want to continue insertion Y/N
Enter the value to be inserted:20
Do you want to continue insertion Y/N
Enter the value to be inserted:30
Do you want to continue insertion Y/N
Enter the value to be inserted:40
Do you want to continue insertion Y/N
The Queue elements are:10
                                                 40
Do you want to perform another operation (Y/N):
Enter your choice for the operation in c deque: 4
The Queue elements are:10
Do you want to perform another operation (Y/N):
```



Multilevel Queue (MLQ)

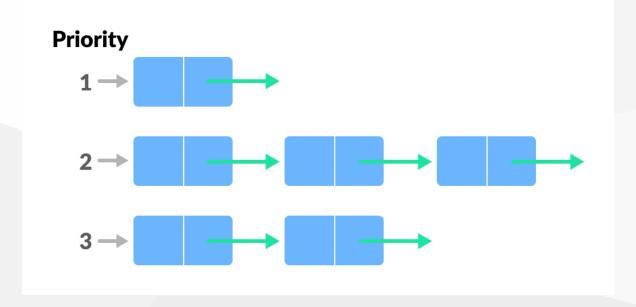
- Geeks for Geeks
 - https://www.geeksforgeeks.org/multilevel-queue-mlq-cpu-scheduling/





Priority Queue

• A priority queue is a special type of queue in which each element is associated with a priority and is served according to its priority. If elements with the same priority occur, they are served according to their order in the queue.



 Insertion occurs based on the arrival of the values and removal occurs based on priority.

Hanoi Tower

- Geeks for Geeks
 - Recursive Version
 - Program for Tower of Hanoi GeeksforGeeks
 - Iterative Version
 - Iterative Tower of Hanoi GeeksforGeeks



Hanoi Tower Iterative Algorithm:

S = Source

A = Aux

D = Dest

Calculate the total number of moves required i.e.

pow(2,n)-1 here n is number of disks.



Hanoi Tower Iterative Algorithm:

- If number of disks (i.e. n) is **even** then interchange **destination pole** and **auxiliary pole**.
- for i = 1 to total number of moves:
 - ∘ if i%3 == 1:
 - legal movement of top disk between source pole and destination pole
 - o if i%3 == 2:
 - legal movement top disk between source pole and auxiliary pole
 - \circ if i%3 == 0:
 - legal movement top disk between auxiliary pole and destination pole



Hanoi Tower Iterative Algorithm

- Tower of Hanoi is a mathematical puzzle where we have three rods (A, B, and C) and N disks.
- Initially, all the disks are stacked in decreasing value of diameter
 - i.e., the smallest disk is placed on the top and they are on rod A.
- The objective of the puzzle is to move the entire stack to another rod (here considered C), obeying the following simple rules
- Only one disk can be moved at a time.
- Each move consists of taking the upper disk from one of the stacks and placing it on top of another stack i.e. a disk can only be moved if it is the uppermost disk on a stack.
- No disk may be placed on top of a smaller disk.

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Hanoi Tower Iterative Algorithm Examples

```
**Input**: 2

**Output:** Disk 1 moved from A to B

Disk 2 moved from A to C

Disk 1 moved from B to C
```

```
**Input:** 3

**Output:** Disk 1 moved from A to C

Disk 2 moved from A to B

Disk 1 moved from C to B

Disk 3 moved from A to C

Disk 1 moved from B to A

Disk 2 moved from B to C

Disk 1 moved from A to C
```



Tower of Hanoi using Recursion

- The idea is to use the helper node to reach the destination using recursion. Below is the pattern for this problem:
 - O Shift N-1 disks from A to B, using C.
 - Shift last disk from A to C.
 - O Shift N-1 disks from B to C, using A.



Tower of Hanoi using Recursion

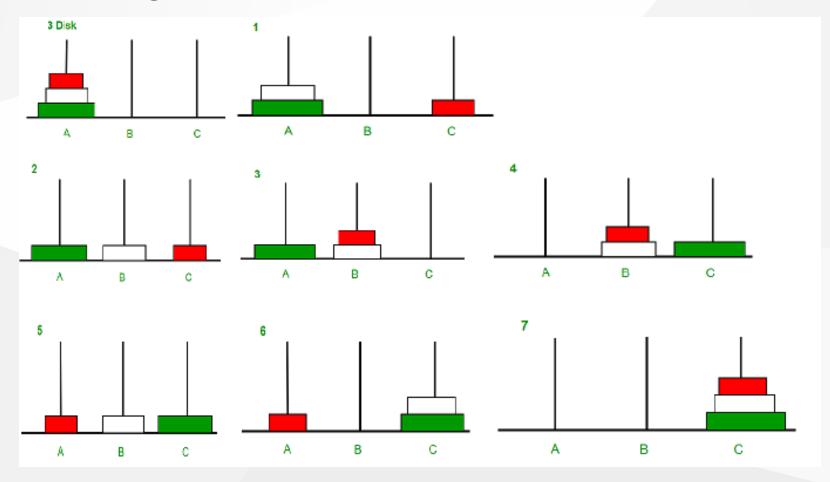


Image illustration for 3 disks



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- Follow the steps below to solve the problem
 - Create a function towerOfHanoi where pass the N (current number of disk), from_rod, to_rod, aux_rod.
 - Make a function call for N 1 th disk.
 - Then print the current the disk along with from_rod and to_rod
 - Again make a function call for N 1 th disk.



```
// C++ recursive function to
// solve tower of hanoi puzzle
#include <bits/stdc++.h>
using namespace std;
void towerOfHanoi(int n, char from_rod, char to_rod,
                char aux_rod)
    if (n == 0) {
        return;
    towerOfHanoi(n - 1, from_rod, aux_rod, to_rod);
    cout << "Move disk " << n << " from rod " << from_rod</pre>
        << " to rod " << to rod << endl;
    towerOfHanoi(n - 1, aux_rod, to_rod, from_rod);
```

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```
// Driver code
int main()
    int N = 3;
    // A, B and C are names of rods
    towerOfHanoi(N, 'A', 'C', 'B');
    return 0;
```

```
// JAVA recursive function to
// solve tower of hanoi puzzle
import java.io.*;
import java.math.*;
import java.util.*;
class GFG {
```



```
static void towerOfHanoi(int n, char from_rod,
                        char to_rod, char aux_rod)
    if (n == 0) {
       return;
   towerOfHanoi(n - 1, from_rod, aux_rod, to_rod);
    System.out.println("Move disk " + n + " from rod "
                    + from rod + " to rod "
                    + to_rod);
    towerOfHanoi(n - 1, aux_rod, to_rod, from_rod);
```

```
// Driver code
public static void main(String args[])
    int N = 3;
    // A, B and C are names of rods
    towerOfHanoi(N, 'A', 'C', 'B');
```



```
// C# recursive program to solve tower of hanoi puzzle
using System;
class GFG {
    static void towerOfHanoi(int n, char from_rod,
                            char to_rod, char aux_rod)
        if (n == 0) {
            return;
        towerOfHanoi(n - 1, from_rod, aux_rod, to_rod);
        Console.WriteLine("Move disk " + n + " from rod "
                        + from_rod + " to rod " + to_rod);
        towerOfHanoi(n - 1, aux_rod, to_rod, from_rod);
```

```
// Driver method
public static void Main(String[] args)
    int N = 3;
    // A, B and C are names of rods
    towerOfHanoi(N, 'A', 'C', 'B');
```



Output

```
Move disk 1 from rod A to rod C
Move disk 2 from rod A to rod B
Move disk 1 from rod C to rod B
Move disk 3 from rod A to rod C
Move disk 1 from rod B to rod A
Move disk 2 from rod B to rod C
Move disk 1 from rod A to rod C
```



Time complexity

- O(2N)
 - There are two possibilities for every disk.
 - Therefore, 2 * 2 * 2 * . . . * 2(N times) is 2N

Auxiliary Space

- O(N)
 - Function call stack space



```
// Assuming n-th disk is
// bottom disk (count down)
class GFG {
static void tower(int n, char sourcePole,
                char destinationPole, char auxiliaryPole)
    // Base case (termination condition)
    if (0 == n)
    return;
    // Move first n-1 disks from source pole
    // to auxiliary pole using destination as
    // temporary pole
    tower(n - 1, sourcePole, auxiliaryPole,
                        destinationPole);
    // Move the remaining disk from source
    // pole to destination pole
    System.out.printf("Move the disk %d from %c to %c\n",
                        n, sourcePole, destinationPole);
    // Move the n-1 disks from auxiliary (now source)
    // pole to destination pole using source pole as
    // temporary (auxiliary) pole
    tower(n - 1, auxiliaryPole, destinationPole, sourcePole);
```

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```
public static void main(String[] args)
{
   tower(3, 'S', 'D', 'A');
}
// This code is contributed by Smitha Dinesh Semwal.
```



```
// Assuming n-th disk is bottom disk
// (count down)
using System;
class GFG {
    static void tower(int n, char sourcePole,
                        char destinationPole,
                        char auxiliaryPole)
        // Base case (termination condition)
        if (0 == n)
            return;
       // Move first n-1 disks from source
       // pole to auxiliary pole using
       // destination as temporary pole
        tower(n - 1, sourcePole, auxiliaryPole,
                            destinationPole);
       // Move the remaining disk from source
       // pole to destination pole
        Console.WriteLine("Move the disk " + n
               + "from " + sourcePole + "to "
                        + destinationPole);
       // Move the n-1 disks from auxiliary
       // (now source) pole to destination
        // pole using source pole as temporary
        // (auxiliary) pole
        tower(n - 1, auxiliaryPole,
               destinationPole, sourcePole);
```



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```
// Driver code
public static void Main()
{
    tower(3, 'S', 'D', 'A');
}
```

```
#include<stdio.h>
// Assuming n-th disk is bottom disk (count down)
void tower(int n, char sourcePole, char destinationPole, char auxiliaryPole)
// Base case (termination condition)
if(0 == n)
    return;
// Move first n-1 disks from source pole
// to auxiliary pole using destination as
// temporary pole
tower(n-1, sourcePole, auxiliaryPole,
    destinationPole);
   // Move the remaining disk from source
// pole to destination pole
printf("Move the disk %d from %c to %c\n",
    n,sourcePole, destinationPole);
// Move the n-1 disks from auxiliary (now source)
// pole to destination pole using source pole as
// temporary (auxiliary) pole
tower(n-1, auxiliaryPole, destinationPole,
    sourcePole);
. . .
```

RECEPTANYIP ET BOOGAN ON IVERSITES RELE

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```
int main()
{
tower(3, 'S', 'D', 'A');

return 0;
}
```

```
// Assuming n-th disk is bottom disk
// (count down)
using System;
class GFG {
    static void tower(int n, char sourcePole,
                        char destinationPole,
                        char auxiliaryPole)
       // Base case (termination condition)
        if (0 == n)
            return;
       // Move first n-1 disks from source
       // pole to auxiliary pole using
        // destination as temporary pole
        tower(n - 1, sourcePole, auxiliaryPole,
                            destinationPole);
       // Move the remaining disk from source
        // pole to destination pole
        Console.WriteLine("Move the disk " + n
                + "from " + sourcePole + "to "
                        + destinationPole);
       // Move the n-1 disks from auxiliary
       // (now source) pole to destination
       // pole using source pole as temporary
        // (auxiliary) pole
        tower(n - 1, auxiliaryPole,
                destinationPole, sourcePole);
```

RECEP TAYYIP ER DOG GAN DON VER STEEL

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```
// Driver code
public static void Main()
{
    tower(3, 'S', 'D', 'A');
}
```

$$End-Of-Week-3$$

